

**Japan-IMF Scholarship Program for Asia 2017-2018**

**Basic Mathematics Aptitude Test**

(Full score: 40)

**Please Note:**

- You have 60 minutes to complete
- No calculator are allowed
- Please show all your work and write your answers in the designated space

*Thank you*

Country: \_\_\_\_\_

Reference Number: \_\_\_\_\_

Name: \_\_\_\_\_

Reference Number: \_\_\_\_\_ Country: \_\_\_\_\_

Name: \_\_\_\_\_

*(Please show all your work here and write your answer in the designated space.)*

[Part 1] (1 point for each question) Answer the following question:

■ **Example questions 1:**

Solve the following expression:

$$\frac{1}{2} + \frac{4}{2}$$

Answer: 2.5 or 5/2

■ **Example questions 2:**

Simplify the following expression:

$$a \times 10 + \frac{a^2}{a}$$

Answer:  $11a$

■ **Now answer the questions below:**

1. Solve the following equation

$$\frac{1}{4} \times 10 + \frac{5}{4} \div \frac{25}{2}$$

Answer: \_\_\_\_\_

2. Given constant  $a$ , simplify the expression below:

$$\frac{a^x (a^x)^{1/2}}{3a^{1-x}}$$

Answer: \_\_\_\_\_

3. Simplify the expression below

$$\ln\left(\frac{x+1}{x-1}\right) + \ln\left(\frac{1}{x+1}\right)$$

Answer: \_\_\_\_\_

4. Solve for  $x$  when

$$e^x e^x = e^{4+x}$$

Answer: \_\_\_\_\_

5. Simplify the expression below

$$\frac{4x^2(5+x)}{20x+4x^2}$$

Answer: \_\_\_\_\_

Reference Number: \_\_\_\_\_ Country: \_\_\_\_\_

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*(Please show all your work here and write your answer in the designated space.)*

**[Part 2] (2 points for each question) Answer the following questions:**

1. Deduce the equation of a line whose slope is 1.2 and which passes through the point (2, 5).

Answer: \_\_\_\_\_

2. Find what values of  $x$  satisfy the inequalities below

$$\begin{cases} 4x - 7 > 3x - 3 \\ 4 - 6x < 12 - 7x \end{cases}$$

Answer: \_\_\_\_\_

3. Solve the following equation

$$\ln(x + 6) = 0$$

Answer: \_\_\_\_\_

4. Find  $x$  satisfying the following equation:

$$\sum_{i=1}^2 ix^{i-1} = 1$$

Answer: \_\_\_\_\_

5. Given constant  $a$  ( $a > 0$ ), find  $x$  satisfying the following equation:

$$a = (x^a)^2$$

Answer: \_\_\_\_\_

Reference Number: \_\_\_\_\_ Country: \_\_\_\_\_

Name: \_\_\_\_\_

*(Please show all your work here and write your answer in the designated space.)*

**[Part 3] (3 points for each question) Answer the following questions:**

1. Given constants  $a$ ,  $b$ , and  $c$ , find the first derivative of the function below:

$$f(x) = 2x^b x^{\frac{a}{2}} + \log c$$

Answer: \_\_\_\_\_

2. Find the second order derivative of the function below:

$$f(x) = \frac{6x - 7}{8x - 5}, \quad (x \neq \frac{5}{8})$$

Answer: \_\_\_\_\_

3. Find the partial derivative  $\frac{\partial^2 f}{\partial x \partial y}$  when  $f(x, y) = (8x - 4y)^5$ .

Answer: \_\_\_\_\_

4. Evaluate the following definite integral.

$$\int_0^2 (3e^x + 5) dx.$$

Answer: \_\_\_\_\_

5. Given constants  $a$ ,  $b$ , and  $c$ , find  $\frac{\partial f}{\partial x}$  when

$$f(x, y) = (ax + by)^b + \ln(xy + 1)^c$$

Answer: \_\_\_\_\_

Reference Number: \_\_\_\_\_ Country: \_\_\_\_\_

Name: \_\_\_\_\_

*(Please show all your work here and write your answer in the designated space.)*

**[Part 4] (5 points for each question) Answer the following questions:**

1. Given  $A = \begin{bmatrix} 4 & 1 \\ 9 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 2 & 0 \\ 7 & 1 \end{bmatrix}$ , and  $C = \begin{bmatrix} 2 & 0 & 1 \\ 1 & 0 & -1 \\ 1 & 2 & 0 \end{bmatrix}$ , answer the following two sub-questions.

(a) **[2 points]** Find  $(AB)'$

Answer: \_\_\_\_\_

(b) **[3 points]** Find the determinant of  $C$ .

Answer: \_\_\_\_\_

2. Answer the following questions:

(a) **[2 points]** Find the local maximum and minimum of the function.

$$f(x) = x^3 - 12x^2 + 36x + 8$$

Answer: \_\_\_\_\_

(b) **[3 points]** Given the function below

$$f(x) = bx^2 - x - c$$

- i. Specify “the condition of the parameter  $b$ ” that this function has a local minimum.
- ii. Find this point.

Answer: \_\_\_\_\_