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## Three Attempts at Inflation Forecasting in Pakistan

*Madhavi Bokil and Axel Schimmelpfennig*

## IMF Working Paper

Middle East and Central Asia Department

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Prepared by Madhavi Bokil and Axel Schimmelpfennig<sup>1</sup>

Authorized for distribution by Milan Zavadjil

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#### Abstract

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This paper presents three empirical approaches to forecasting inflation in Pakistan. The preferred approach is a leading indicators model in which broad money growth and private sector credit growth help forecast inflation. A univariate approach also yields reasonable forecasts, but seems less suited to capturing turning points. A vector autoregressive (VAR) model illustrates how monetary developments can be described by a Phillips-curve type relationship. We deal with potential parameter instability on account of fundamental changes in Pakistan's economic system by restricting our sample to more recent observations. Gregorian and Islamic calendar seasonality are addressed by using 12-month moving averages.

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Author(s) E-Mail Address: madhavi@ucsc.edu; aschimmelpfennig@imf.org

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<sup>1</sup> Madhavi Bokil was a summer intern at the IMF when this paper was initiated; she is currently at the University of California at Santa Cruz. The authors would like to thank Ashfaque Khan, Jorge Canales-Kriljenko, Abdul Naseer, Milan Zavadjil, and participants at a MCD Economist Research Club Seminar for their valuable comments.

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## I. INTRODUCTION

**Inflation forecasts can be important monetary policy formation.** For most central banks, inflation is at least one monetary policy objective. Given typical time lags, monetary policy needs to be concerned with future inflation. Current inflation levels, which are themselves the result of past policies, may provide only insufficient information. Inflation forecasts that link future inflation to current developments can bridge this gap. Some central banks have even adopted an inflation forecast target. However, this assumes that inflation forecasts are very reliable. Still, even in situations where structural relationships are less stable and data quality is still evolving, quantitative inflation forecasts can provide useful information on future developments that need to be combined with additional analysis going beyond econometrical relationships. This paper attempts to develop an inflation forecasting model for Pakistan that could serve as input for policy setting by the State Bank of Pakistan (SBP).

**Monetary policy in Pakistan is charged with three objectives.** According to the SBP's July 2004 monetary policy statement (see page 5), monetary policy "... will have to ensure that the current growth and investment momentum in the country is not impaired in any significant manner, export competitiveness is maintained while inflation is kept under control." The SBP has operationalized these objectives as quantitative targets. The inflation target for 2004/05 was 5 percent, though it has subsequently been raised to 7 percent. The SBP has also adopted the government's growth targets of 6.5 percent in 2004/05, increasing to 8 percent over the medium term. Lastly, the SBP tries to smooth excess exchange rate volatility, at times giving the impression of supporting certain psychological thresholds for the Pakistani rupee–U.S. dollar rate. More generally, the SBP looks at competitiveness when assessing the exchange rate. At times, these objectives can be conflicting and thus difficult to achieve simultaneously using only monetary policy instruments.

**Data availability together with potential parameter instability are the main challenges to forecasting inflation.** Pakistan's national accounts are compiled on an annual basis, so that only a few, mostly monetary variables, are available at high frequency and with short lags. In addition, we find several structural breaks in long time series reflecting fundamental policy framework changes that are difficult to model explicitly. We address these challenges by truncating our sample and including only recent observations that do not include severe structural breaks. In order to still have a reasonably large sample size, we use monthly data, which limits our choice of variables to monetary variables, and a manufacturing index that serves as a proxy for activity.

**This paper presents three empirical approaches to forecasting inflation in Pakistan.** The preferred approach is a leading indicators model (LIM) in which broad money and private sector credit growth lead inflation by more than six months. A vector autoregressive model (VAR) illustrates how monetary developments can be described by a Phillips-curve type relationship. A univariate approach (auto-regressive integrated moving average, ARIMA) seems less suited to capturing turning points. While far from perfect, the LIM may be helpful to inform monetary policy formulation.

**The remainder of the paper is organized as follows.** Section II briefly surveys literature on inflation forecasting and summarizes empirical work on inflation and money demand in Pakistan. Section III describes the data and illustrates the potential parameter instability based on a simple money demand function. Section IV presents the three forecasting models, and Section V concludes.

## II. A SELECTIVE LOOK AT THE LITERATURE

### A. Determinants of Inflation

**There is a large and growing literature on inflation forecasting in emerging market economies.** Similar to the findings for advanced economies, changes in money growth, nominal exchange rates, price of imports, inflation expectations, and exogenous supply shocks, especially to oil and food prices, are identified as the main determinants of inflation in emerging market economies.<sup>2</sup> This is consistent with theoretical work that views inflation to be a monetary phenomenon in the long run when prices and wages are flexible and output and employment are always at their natural rates, but in the short run, models inflation as being also driven by real and nominal shocks that affect aggregate demand relative to aggregate supply.

**There are several theoretical starting points for empirical inflation forecasting models.** The Phillips curve has been used extensively in inflation forecasting, linking inflation to some measure of real economic activity such as the unemployment rate. When forecasting is the objective, Stock and Watson (1989) show that going beyond a single model such as the Phillips curve and including a wide set of potential explanatory variables leads to a better model in terms of forecast accuracy. Monetary variables, e.g., based on a money demand function can serve as additional explanatory variables in an inflation forecasting model. Monetization of the fiscal deficit can also contribute to inflation, though Fischer, Sahay, and Végh (2002) find a strong relationship between fiscal deficits and inflation only for high inflation countries or during high inflation episodes. In open economies, inflation can result from movements in the nominal exchange rates. Finally, inflation expectations and their formation can impact inflation through price-wage spirals or inertia.<sup>3</sup>

### B. Empirical Studies for Pakistan

**A large number of empirical studies is available that looks at inflation and monetary policy relationships in Pakistan.** Some studies are based on samples going back as far as

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<sup>2</sup> For example, Chauvet (2000) and International Monetary Fund (2001) for Brazil, Leigh and Rossi (2002) for Turkey, Sun (2004) for Thailand, Coe and Mc Dermott (1997), Simone (2000), and Bailliu, Garcés, and Kruger (2003).

<sup>3</sup> Other studies have looked at the term structure (e.g., Estrella and Mishkin, 1997) or asset prices (e.g., Goodhart and Hofman, 2000) as variables that help forecast inflation.

the 1950s, but most start in 1972, using either annual or constructed quarterly data. Most studies employ either cointegration techniques or estimate vector autoregressive models (often in first differences). All studies are in the business of model building and none attempts to use their results for forecasting. Table 1 provides a survey of the literature.

**Most empirical studies find standard economic relationships to hold.** Estimates of money demand functions mostly find money demand to be determined by measures of opportunity costs and activity (e.g., Tariq and others, 1997). Likewise, inflation is influenced by changes in money supply, interest rates, measures of aggregate demand or output, and import prices (e.g., Ahmad and Ali, 1999a). While most studies find such relationships to hold in a cointegration framework, a few fail to find cointegration which could suggest structural breaks in particular samples (e.g., Shamsuddin and Holmes, 1997). There seems to be no or only little exchange rate pass-through to domestic prices (e.g., Choudhri and Khan, 2002).

### III. DATA AND SAMPLE

**Three main challenges to developing a forecasting model arise with respect to the data.** First, ongoing changes in Pakistan's financial system such as financial deepening imply that simple standard relationships such as money demand functions may not be stable at the end of the sample period. Second, only a few, mostly monetary, variables are available on a monthly or quarterly basis.<sup>4</sup> Third, Pakistan's data is not only subject to Gregorian calendar effects, but also to Islamic calendar effects.<sup>5</sup> Our choice of variables and their transformations are largely motivated by these challenges.

**The database includes mostly monetary and financial data available at monthly frequency.** We restrict the analysis to monthly data because this is available with much shorter lags and thus more suitable for a continuous forecasting exercise. Moreover, this also gives us a sufficient number of observations and thus degrees of freedom even though we do not extend our sample before 1998. However, restricting ourselves to monthly data implies that we cannot use variables such as GDP because national accounts are compiled only on a fiscal year basis. As such, data is restricted to monetary aggregates, interest rates, the exchange rate, and inflation. In addition, we use the monthly large-scale manufacturing index to proxy activity. Table 2 presents descriptive statistics for the core variables in our database.

#### A. Seasonality and Stationarity

**We address seasonality by using 12-month moving averages.** Using average annual inflation as well as 12-month averages for possible regressors in the VAR and the LIM smoothes out calendar year effects. In addition, averaging should also smooth out Islamic calendar effects, except for the rare case where, for example, two Eids fell into one calendar

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<sup>4</sup> GDP, for example, is available only annually, though quarterly national accounts are under construction.

<sup>5</sup> Prices tend to increase during Ramadan and the Eids (religious holidays).

year.<sup>6</sup> For the ARIMA, we also test whether inclusion of Islamic calendar dummies improves the estimated model.

**Using 12-month moving averages has other advantages.** Inflation targets are typically set for average annual inflation (or core inflation), though this may be combined with a path for year-on-year or month-on-month inflation. In this sense, the forecast of average annual inflation is directly applicable to the policy discussion without having to convert a forecast trajectory for year-on-year inflation into an annual average inflation. In addition, 12-month moving averages are likely to be less volatile than monthly observations that can be subject to temporary erratic shocks.

**Most core variables in the database are nonstationary in levels** (Table 3). In our sample range, the consumer price index (CPI), broad money, credit to the private sector, the six-month treasury-bill rate and the output gap<sup>7</sup> are integrated of order one based on augmented Dickey-Fuller (ADF) tests. However, reserve money and the large scale manufacturing index are stationary. Inflation is found to be integrated of order two by the ADF test. While this is not unusual, it seems somewhat at odds with the finding that the CPI is integrated of order one. Moreover, a graphical inspection of the inflation series casts some doubt on this result as does the Phillips-Perron test. Private sector credit growth is found to be stationary by both tests which is also surprising given its high correlation with broad money growth. When interpreting these results it is important to bear in mind that tests for nonstationarity are biased toward nonrejection in small samples.

## B. Sample and Structural Breaks

**We mostly restrict the sample to July 1998 onwards.** This starting point was chosen to exclude observations before the 1998/99 crisis after which the exchange rate was liberalized substantially and financial policies were targeted at macroeconomic stabilization. A casual look at the data supports this cut off date as inflation appears to be much more stable since the crisis. Truncating the sample in 1998 has the added advantage that the recent fundamental changes in the financial system would be better reflected in the estimated coefficients which should contribute to better forecasts. However, nonconstant coefficients remain a problem for at least one of our approaches. At the time of estimation, the latest available observation was December 2004 for some variables which leaves a fairly short sample.

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<sup>6</sup> Several standard techniques are available to address Gregorian calendar seasonality. However, only little work has been done to address Islamic calendar effects that cannot be controlled for by standard techniques which are calendar year-based because the Islamic year is shorter than the calendar year. A notable exceptions is Riazuddin and Khan, 2002.

<sup>7</sup> We calculate the output gap as the difference of the large scale manufacturing index from its long-run trend in percent of the trend.

**Pakistan has undergone several distinct policy framework changes over the last three decades.** The Pakistani rupee was fixed against the U.S. dollar in the 1970s and was floated in 1982. Throughout the 1980s and 1990s, the Pakistani rupee depreciated against the U.S. dollar, peaking during the 1998/99 debt crisis. Since then, the SBP has pursued a managed float policy. Monetary policy relied on credit plans to the public and private sector in the 1970s and 1980s. Interest-free banking was partially introduced in 1981 and interest-bearing deposits of banks were replaced by a profit and loss sharing system in 1985. In 1989, Pakistan started on a financial sector reform program that involved interest rate liberalization, reduction of credit controls, and strengthening the supervisory framework. During the 1989/99 debt crisis, the SBP had to temporarily freeze foreign currency deposits and imposed exchange controls that were subsequently lifted again. Financial sector reforms gained momentum after the debt crisis. Today, the SBP uses t-bill auctions as the main monetary policy instrument. The SBP also operates a discount window and carries out open market operations as needed for liquidity management purposes and to support the general monetary policy direction. The SBP does not publish a quantitative inflation forecast, but the semiannual monetary policy statement includes an inflation target and discusses prospects for achieving the target.

**Ongoing financial deepening changes the environment for monetary policy.** The SBP has moved away from targeting monetary aggregates such as reserve money and net domestic assets (NDA). In the past few years, NDA targets agreed under the Fund program were not effective in controlling reserve money growth because of the strong net foreign asset accumulation that continued to outperform projections. Instead, the SBP has relied increasingly on short-term interest rates to achieve its objectives. With steady improvements in financial intermediation and continued financial deepening, the credit channel should become more effective, strengthening short-term interest rates as the main policy instruments. Our finding below that private sector credit growth is a good leading indicator for inflation is evidence that the credit channel is part of the monetary transmission mechanism in Pakistan.

**A casual look at monetary and inflation developments indicate that standard relationships may not always hold, in particular for more recent observations** (Figures 1 and 2). Since 2000/01 (July–June), broad money, credit to the private sector, as well as currency in circulation have grown much faster than nominal GDP. At the same time, inflation has dropped from its average of above 10 percent in the early 1990s to below 5 percent in 2002/03. Though, more recently, inflation has increased again to about 7 percent at the end of 2004. One reason for these developments is likely to be the process of financial deepening that has occurred since 1999. Reforms have substantially strengthened the banking sector and have lead to large improvements in financial intermediation (cf. International Monetary Fund, 2004). A closer inspection of the CPI inflation time series suggests that a structural break may have occurred somewhere around the 1998/99 debt crisis.



**Estimating a simple money demand function with annual data from 1975 through 2004 illustrates parameter instability.** As a preliminary exercise, we estimate a money demand function based on the quantity equation.

$$\ln P = -\ln v + \beta_1 \ln M - \beta_2 \ln Y$$

where  $P$  is the CPI,  $v$  the velocity,  $M$  broad money, and  $Y$  real GDP. For this exercise, we use annual data from the IMF's *International Financial Statistics* database from 1975 through 2004. All coefficients carry the expected sign: the constant, that is the log of velocity is negative, an increase in broad money raises the CPI, and an increase in real GDP reduces the CPI (Table 4).<sup>8</sup> However, the coefficient on real GDP is not significant. Calculating recursive estimates for the coefficients clearly exhibits parameter instability (Figure 3). In the case of real GDP, the coefficient even switches signs from positive to negative. The recursive coefficients suggest two break points. The first one occurs around 1992 when Pakistan floated the Pakistani rupee, and the second one seems to occur around 1999 when financial policies were directed toward macroeconomic stabilization after the 1998/99 debt crisis.

**These results are confirmed when using monthly data from 1995 through 2004.**<sup>9</sup> Instead of real GDP, we use a manufacturing index available on a monthly basis.<sup>10</sup> Again, all coefficients carry the expected sign, and in this case, all are significant at all standard levels (Table 5).<sup>11</sup> The recursive coefficients point to structural breaks around 1997 and again in 1999/2000; there is also a sign switch at the beginning of the sample period for the manufacturing index (Figure 4). Maybe most interestingly, the estimate of the velocity increases from around 0.004 in 1996 to 0.08 in 2004 which would be consistent with financial deepening.

**For our purposes of developing an inflation forecasting model, we try to overcome this parameter instability by restricting our sample to the period of 1998 onwards.** The above parameter instability could be addressed in two ways. We could attempt to explicitly model the structural changes such as financial deepening. However, given the scarcity of available data, we are doubtful whether this can be done sufficiently well to yield a good forecasting model. Therefore, we choose to focus our empirical work on more recent episodes that are not subject to distinct structural breaks. This has to be balanced by the need

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<sup>8</sup> Given that all time series are integrated of order one, the least squares regression should be viewed as the first stage of the Engle/Granger approach. Using the standard cointegration test based on the regression residuals, the null hypothesis of cointegration is not rejected.

<sup>9</sup> All variables are 12-month moving averages to account for Gregorian and Islamic calendar seasonality.

<sup>10</sup> The correlation coefficient between the annual manufacturing index and real GDP is 0.97 which suggests that a 12-month moving average of the manufacturing index should be a reasonable proxy for monthly GDP.

<sup>11</sup> The null hypothesis of cointegration is not rejected.

to have a sufficiently large sample for the estimation. Based on some initial and preliminary work, we restrict our sample to observations from July 1998 onwards.

#### IV. THREE FORECASTING APPROACHES

**We use three empirical approaches to forecasting inflation.** As a benchmark, we estimate a univariate ARIMA model. Next, we use a VAR model that includes several variables based on an economic model. And finally, we use a LIM, which less concerned with mirroring an economic model. We find the LIM to be best suited for forecasting in terms of statistical properties and measures of forecast accuracy. However, once longer time-series become available, we believe that an economic model-based VAR could allow more in-depth policy analysis.

##### A. A Univariate Forecasting Model

**In the simplest form, inflation can be modeled as an ARIMA process.** We determine the optimal lag length according to the Box-Jenkins methodology, significance tests, and statistics measuring the forecast quality such as the root square mean error. Even though the CPI itself is integrated of order 1, average annual CPI inflation also appears to be integrated of order 1. Therefore, we differentiate average annual inflation once. We have also experimented with ARMAs for average annual inflation and 12-month inflation, but the results did not improve upon what is presented here.

**We estimate the following ARIMA(p,1,q) model**

$$\Delta \dot{P}_t = \alpha_0 + \sum_{i=1}^p \alpha_i \Delta \dot{P}_{t-i} + \sum_{j=0}^q \gamma_j u_{t-j}$$

where  $\dot{P}$  denotes average annual CPI inflation and  $u$  denotes a white noise error term.

**The best specification is an ARIMA(5,1,1) model which delivers reasonable predictions.** The autocorrelation function slowly dampens and becomes insignificant at lag 6, while the partial autocorrelation function breaks off after lag 1 (Figure 5). This suggests and ARIMA(6,1,0). However, looking at information criteria, root mean square error and similar statistics suggests an ARIMA(5,1,1) (Table 6).<sup>12</sup> Reestimating the ARIMA(5,1,1) for a reduced sample through June 2004 allows us to forecast for the remainder of 2004 and compare the forecast to the actual developments (Figure 6). The forecast has inflation increasing during July–December 2004, but not as fast as actual inflation did increase. As such, actual inflation is consistently above the 2-sigma band. Still, while the forecast fails to anticipate the extent by which inflation increased, it does anticipate the increase itself. In

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<sup>12</sup> Doing a wider search for the best lag structure based on the information criteria, root mean squared error and other related statistics suggests an ARIMA(11,1,11) as the best model. However, in terms of actual forecast, this specification does no better than the ARIMA(5,1,1) and we thus prefer the more parsimonious specification.

earlier work for a shorter sample, ARIMA models had difficulties anticipating turning points—unsurprisingly as they do not explicitly model exogenous shocks.

**Including Islamic calendar dummies in the ARIMA(5,1,1) does not improve the forecast quality.** We use four Islamic calendar dummies constructed by Riazuddin and Khan (2002).<sup>13</sup> The four dummies control for effects related to *Muharram*, *Ramashan*, *Shawal*, and *Thul Hujja* and take on values between zero and one depending on how many days of a particular holiday fall into a month. Unfortunately, including these dummies does not improve the model's forecast quality (Figure 7), and the dummies themselves are estimated as insignificant at the 5 percent level (Table 7). We interpret these results to mean that using 12-months averages sufficiently addresses Islamic calendar effects.

### B. An Unrestricted Vector Autoregressive Model

**A VAR allows a more model-based approach that should be better able to identify shocks that may trigger turning points in inflation.** With nonstationary variables, the VAR can be specified as a vector error correction model in levels that separates long-run and short-run relationships. However, we failed to find cointegration in various specifications which is likely to reflect the fairly short sample span that does not provide sufficient information on long-run relations as well as the structural changes taking place in the financial system. Therefore, we specify a VAR in first differences that describes only short-run relationships. Parameter restrictions would be required to make the VAR truly model-based. However, for now, we have only estimated an unrestricted VAR. The VAR's lag length is selected based on standard information criteria and tests for normality of the error terms; the information criteria suggest a lag length of one, but we set the lag length at three to ensure that the residuals are white noise.<sup>14</sup>

**The widely used Phillips curve provides the theoretical starting point.** We estimate a three-dimensional VAR that includes the inflation rate, the output gap, and the real interest rate. We define the real interest rate as the difference between the 3-month t-bill rate and expected inflation where inflation expectations are based on a simple ARMA model. Alternatively, we used the nominal t-bill rate which resulted in the fairly common finding of a price puzzle where an unexpected tightening in monetary policy leads to an increase rather than a decrease in the price level. Introducing a forward looking variable addresses this theoretical inconsistency (e.g. Brissimis and Magginas, 2004), in our case this is the expected real interest rate.<sup>15</sup>

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<sup>13</sup> We thank the authors who kindly provided this data for our work.

<sup>14</sup> Specifically, we relied on the Schwartz information criterion, the Akaike information criterion and the Hannan-Quinn information criterion to determine the lag-length.

<sup>15</sup> See Giordani (2004) and Balke and Emery (1994) for a discussion of the price puzzle finding.

**We need to further curtail the sample for the VAR estimation.** When starting the sample in July 1998, we cannot identify a meaningful VAR specification that satisfies standard statistical criteria. A look at a time series chart for inflation and the output gap reveals why this might be the case (Figure 8). The typical relationship where a closing output gap puts upward pressure on inflation only emerges after July 2001. Therefore, we start the sample for the VAR estimation only in July 2001 which leads to more interesting results. However, the very small sample size severely limits the quality of these results.

**The estimation results are shaky, but provide some insights.** Our preferred specification is a VAR including inflation, a real interest rate (defined as the 3-month t-bill rate less expected inflation from an ARMA model), and the output gap. In this specification, inflation is low when the output gap is large (negative) or when the real interest rate is high (Table 8). However, there is no feedback between output gap or real interest rate in either direction.<sup>16</sup> The estimated output gap equation does not fit the data well. Reestimating the model for a reduced sample through March 2004 and comparing the forecast with actual data, shows that the VAR forecast does not capture the accelerating trend of inflation, though actual inflation is within the wide 2-sigma band (Figure 9).

**As typical economic relationships are firming up in the data, the VAR approach should become a useful tool to forecast and analyze inflation trends.** At present, not enough data is available to estimate a structural VAR with sufficient precision. Moreover, structural changes in the financial system result in nonconstant coefficients which make forecasting problematic. However, after 2001, Phillips curve-type relations are found in the data. If these relations were to firm up going forward, a structural VAR that reflects an economic model should provide a powerful tool for forecasting inflation and analyzing monetary policy.

### C. Leading Indicators Model

**The leading indicators approach searches for variables that co-move with the variable to be forecasted without imposing a model structure.** Leading indicators do not necessarily need to be causal factors of the target variable as part of an economic model, though this would presumably strengthen one's confidence in a forecasting model (e.g., Marcellino, 2004, and Stock and Watson, 1989 and 1999). We use the general-to-specific algorithm in PcGets to narrow down the set of possible leading indicators from our full dataset and then use the same criteria of forecast accuracy as for the ARIMA to arrive at a final specification (see Hendry and Krolzig, 2004). We require indicators to lead inflation by at least 6 months and allow for leads up to 12 months.

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<sup>16</sup> This can also be seen from impulse-response functions based on a Cholesky decomposition. The ordering of the variables does not matter for this result as the off-diagonal elements of the correlation matrix are close to zero.

**Private sector credit growth and broad money growth are leading indicators of inflation** (Table 9). The general model includes the following variables that could be leading indicators for inflation: wholesale-price index inflation, time-varying intercept, and slope coefficient for the yield curve, the spread between 12-month and 3-month t-bill rates, large-scale manufacturing index growth, broad money growth, reserve money growth, private sector credit growth, change in the nominal effective exchange rate, tax revenue growth, and the 6-month t-bill rate. Of these, only private sector credit growth and lags of inflation remain in the reduced specification (Model 1).<sup>17</sup> We also show specifications that include broad money growth as one might expect a relationship between broad money growth and inflation. The best specification here is model 3 which includes lags of broad money growth and private sector credit growth in addition to lags of inflation. Both specifications are consistent with a monetary transmission mechanism that works through the credit channel.

**The LIMs' exhibit a good ex-post forecast quality.** Reestimating the LIMs through May 2004 and forecasting the remainder of 2004 allows a comparison of the models' forecast with actual developments (Figure 10). The ex-post forecast based on Model 1 (private sector credit growth) seems a bit closer to actual developments than the ex-post forecast based on Model 3 (private sector credit growth and broad money growth). However, the ex-post forecast based on Model 3 has a lower standard error.

**The LIMs do not suffer from parameter instability.** Figures 11 and 12 show recursive coefficient estimates for Model 1 and 3. In both cases, the coefficient estimates do not fluctuate much once the sample has reached a certain size, and the coefficient estimate for the full sample remains mostly in the 2-sigma band around the recursive coefficient estimates.

**The leading indicators models yield a fairly accurate forecast, but are not firmly grounded in an economic model.** By construction, the approach picks leading indicators that yield a high forecast accuracy at the current juncture. Moreover, higher broad money growth and higher private sector credit growth being associated with higher inflation seems plausible from an economic point of view. However, the choice of leading indicators may change over time, so that the forecasting model may not be stable. As such, periodic respecification and reestimating would be required.

## V. SUMMARY AND CONCLUSIONS

**Pakistan's economic data permits quantitative forecasts of inflation.** High frequency data for Pakistan is largely restricted to monetary data. Only few real sector variables are available at a sub-annual basis. The monthly large-scale manufacturing index, which is correlated with real GDP, is a notable exception. Models that build on longer time series going back before the 1998/99 debt crisis suffer from parameter instability associated with

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<sup>17</sup> Detailed results available from the authors upon request.

structural and economic regime changes in Pakistan. Nonetheless, we found that the available monthly data from 1998 onward is sufficiently rich to allow inflation forecasting.

**The leading indicators approach seems most suited for inflation forecasting at this time.**

We presented two variants of a leading indicator model that performed well in ex-post forecasts and could be related back to economic transmission channels. The univariate approach also resulted in a fairly acceptable forecasting model, though the ARIMA's forecasting accuracy was much less than the LIMs'. The model-based VAR approach yielded the least satisfactory forecasting model, but provided some first glances at the evolving monetary transmission mechanism. Given the ease of computing, it is possible to simultaneously use both LIM variants and the ARIMA for forecasting. The LIM based on broad money growth and private sector credit growth as well as lags in inflation may be a natural candidate for the "central" forecast since it almost nests the LIM based on private sector credit growth and lags in inflation as well as the ARIMA.

**A forecasting model based on economic theory would be useful to analyze and simulate monetary policy.**

Our preferred forecasting models are largely driven by statistical properties and less by economic intuition. As such, there is limited scope to use these models to analyze monetary policy in more detail. For example, it is strictly speaking not possible to invert the leading indicators model to derive by how much monetary growth would have to be reduced to achieve a certain inflation target. As economic relationships in Pakistan firm up, a structural VAR approach to inflation forecasting should become feasible, which would yield a richer forecast that will also allow an analysis of the impact of monetary policy instruments.

**The models presented here can be developed further.** In part, this will require longer time series, but also some stabilization in the rapidly developing financial system to ensure parameter stability. Given the data limitations, our econometric techniques were also constrained, and we look forward to future refinements. In the meantime, we can put our LIM-based forecasts to the test of time.

**Fairly simple forecasting models can still be quite powerful.** Looking beyond Pakistan, our paper suggests that it does not necessarily take a lot of data or long time-series to come up with a decent forecasting model. In many cases, it is not possible to explicitly model exogenous changes that lead to parameter instability because there is not enough data or the required model would be too complex for forecasting purposes. Restricting the sample to more recent observations is one alternative that can work. Of course, this comes at the cost of losing information (and degrees of freedom). Moreover, this may require frequent respecification of the forecasting model if the economy continues to undergo changes. The leading indicators approach combined with the general-to-specific algorithm in PcGets lend themselves to the application in data scarce environments. The algorithm allows to work through a large number of specifications do not necessarily have to be nested in one single equation if this is not possible because of a small sample size.

Table 1. Pakistan: Empirical Studies of Inflation and Monetary Policy

| Authors  | Empirical Approach  | Dependent Variable  | Regressors  | Sample Period  | Findings  |
|--|---|---|---|--|---|
| Hyder, Zulfiqar and Sardar Shah (2004)             | VAR   | CPI inflation, WPI inflation, PR/USD, M2, LSM index, oil prices | 1988:I to 2003:9  | Little exchange rate pass through to domestic CPI inflation. |   |
| Choudhri, Ehsan U. and Mohsin S. Khan (2002)       | Single equation and VAR in first differences  | CPI and WPI   | U.S. dollar exchange rate, foreign price index                                | 1982–2001  | There is no exchange rate pass-through to domestic prices.  |
| Ahmad, Eatqaz and Muhammad Mumirs (2000)           | OLS, cointegration analysis   | M1, M2  | Index of industrial production, interbank call money rate, CPI inflation      | 1972:I to 1996:I   | Find that inflation is a better measure of opportunity cost than interest rate, money demand adjusts sluggish, and there was a structural break in the early 1990s. |
| Ahmad, Eatqaz and Saima Ahmed Ali (1999a)          | Single equation, including Engle/Granger cointegration test, 2-equation model with 2SLS | CPI and exchange rate   | Exchange rate, import prices, world prices, money supply, GDP, forex reserves | 1982:II to 1996:IV   | CPI reacts to changes in import prices (due to change in world prices or exchange rate) and money supply. Exchange rate responds to domestic and world prices.      |
| Ahmad, Eatqaz and Saima Ahmed Ali (1999b)          | 2-equation model with 2SLS  | CPI and exchange rate   | Exchange rate, import prices, world prices, money supply, GDP, forex reserves | 1982:II to 1996:IV   | CPI reacts to changes in import prices (due to change in world prices or exchange rate) and money supply. Exchange rate responds to domestic and world prices.      |
| Price, Simon and Anjum Nasim (1999)                | Johansen (VECM), and SUR  | CPI and exchange rate   | Broad money, world prices, GDP, deposit rate                                  | 1974 to 1994   | PPP and money demand relation are identified that are connected through cointegrating relationships.  |
| Hsing, Yu (1998)                                   | Single equation   | Real M2   | Real GDP, deposit rate  | n.a.   | Real GDP elasticity is close to unity whereas interest elasticity is low.   |
| Shamsuddin, Abul F.M. and Richard A. Holmes (1997) | Johansen procedure, VARMA, ARMA   | CPI   | Broad money, real output  | 1972:II to 1993:IV   | Rejects a cointegrating relationship between inflation, broad money and GDP and concludes that a univariate ARMA yields the best forecasts.                         |

Table 1. Pakistan: Empirical Studies of Inflation and Monetary Policy (continued)

| Authors                                       | Empirical Approach                         | Dependent Variable | Regressors  | Sample Period        | Findings  |
|---|--|--------------------|---|----------------------|---|
| Tariq, Syed Muhammed and Kent Matthews (1997) | Johansen, single equation ECM              | M2, M1, divisia    | Real GDP, opportunity costs   | 1974:IV to 1992:IV   | Identifies a cointegration vector that is interpreted as a money demand function. Short-run parameters of money demand equation are stable.   |
| Chaudhary, M. Aslam and Naved Ahmad (1996)    | OLS  | CPI inflation      | Broad money, GDP growth, share of service sector, public debt, import prices  | 1972 to 1992         | Inflation results from money growth and structural factors such as growth, share of service sector, public debt, and import prices.   |
| Arize, A.C. (1994)                            | OLS of ECM                                 | M1, M2             | GDP, inflation rate, call money rate, government bond yield, expected rate of depreciation (foreign interest differential)  | 1973:I to 1990:I     | Finds that money demand is a function of GDP, inflation, interest rate and exchange rate expectations. Also, dummies for the oil shocks, and structural breaks in 1981 on account of introduction of partial interest-free banking and floating the rupee matter. |
| Hossain, Akhtar (1994)                        | Engle/Granger 2-stage, Johansen            | M1, M2             | GDP, yield on government bonds, market call rate, CPI inflation   | 1951-91              | Meaningful cointegration relationship (money demand function) for the post-1972 period.   |
| Khan, Ashfaq H. (1994)                        | Engle/Granger 2-stage                      | M1, M2             | Real income, real interest rate (short-term and medium-term), nominal interest rate (short-term and medium-term), inflation | 1971:III to 1993:III | Finds cointegrating relationship between M2 (or M1) and real income, real interest rate and inflation.  |
| Dhaka, Dharmendra and Magda Kandil (1993)     | OLS of distributed lag specification (AIC) | CPI inflation      | M1, industrial production, interest rate, foreign interest rate, import prices  | 1970:I to 1987:IV    | Import prices, industrial production, and U.K. interest rate explain inflation. M1 is insignificant.  |



Table 1. Pakistan: Empirical Studies of Inflation and Monetary Policy (continued)

| Authors  | Empirical Approach                                    | Dependent Variable  | Regressors  | Sample Period      | Findings   |
|--|---|---|---|--------------------|--|
| Khan, Imran Naveed (1992)                        | OLS   | M1, M2  | GNP, call rate, CPI   | n.a.               | Money demand in Pakistan is a function of income and inflation, but not of interest rate.  |
| Ahmad, Eatjaz and Harim Ram (1991)               | OLS   | WPI, CPI, GNP deflator, and absorption deflator inflation | Real GNP growth, growth rate of unit value of imports, growth rate of M1/M2, lagged inflation | 1960 to 1988       | Inflation is determined by real GNP growth, unit value of import growth, nominal money growth, and lagged inflation.                                     |
| Ahmad, Mushtaq and Ashfaq H. Khan (1990)         | ML (Cooley/Prescott 1976 varying parameter technique) | M1, M2  | Income, inter-bank call rate, time deposit rate   | 1959 to 1987       | Demand for real money was unstable at the time of delinking the Pakistani rupee from the U.S. dollar and introduction of interest-free deposit accounts. |
| Burney, Nadeem A. and Mohammad Akmal (1990)      | NLLS  | Real money stock  | Income, CPI inflation, CPI inflation volatility   | n.a.               | Real money adjusts instantaneously to the desired level of money demand which is driven by income, and expected inflation.                               |
| Khan, Ashfaq H. and Bilquees Raza (1989)         | OLS   | M1, M2  | Real GNP, interest rate, expected inflation   | 1972:II to 1987:II | Larger than unity income elasticities of money demand and the expected influence of expected inflation and interest rates.                               |
| Huq, M.D. Shamsul and Majumdar, Badiul A. (1986) | OLS   | M1, M2  | GNP, call money rate, government bond rate, CPI inflation                                     | 1955 to 1977       | Structural breaks in the demand for money in 1965 and 1971.  |
| Nisar, Shaheena and Naheed Aslam (1983)          | OLS   | M1, M2  | GNP, term structure, GNP deflator   | 1959 to 1978       | Term structure matters for money demand besides income.  |
| Khan, Ashfaq (1982a)                             | OLS   | M1, M2  | GNP, interest rate on time deposits   | 1959/60 to 1979/80 | Income elasticity of 1.7 and interest elasticity of 0.5.   |

Table 1. Pakistan: Empirical Studies of Inflation and Monetary Policy (concluded)

| Authors   | Empirical Approach      | Dependent Variable | Regressors                                     | Sample Period      | Findings   |
|---|-------------------------|--------------------|--|--------------------|--|
| Khan, Ashfaq H. (1982b)                               | OLS                     | M1, M2             | GNP, expected inflation, inflation variability | n.a.               | Including the variability of inflation improves the estimate of the money demand function.                         |
| Naqvi, Syed Nawab, A.R. Kemal, and Rashid Aziz (1982) | 53-equation macro model |                    |  | 1959/60 to 1978/79 | Inflation is not imported. Money demand is interest-sensitive. The GNP elasticity of money demand is fairly large. |

Table 2. Pakistan: Descriptive Statistics

(Average annual change in percent unless otherwise indicated)

|                                 | Mean | Median | Minimum | Maximum | Standard<br>Deviation |
|---------------------------------|------|--------|---------|---------|-----------------------|
| Inflation                       | 4.2  | 3.9    | 2.4     | 7.4     | 1.4                   |
| Broad money                     | 12.5 | 12.2   | 4.3     | 19.2    | 4.8                   |
| Reserve money                   | 12.5 | 12.7   | 8.5     | 17.5    | 2.5                   |
| Credit to the private sector    | 12.4 | 12.3   | 1.7     | 30.4    | 8.1                   |
| 6-months treasury bill rate     | 7.6  | 7.6    | 1.2     | 15.6    | 4.1                   |
| Large-scale manufacturing index | 7.8  | 6.3    | -21.1   | 47.0    | 12.2                  |
| Output gap 1/                   | -0.4 | -1.9   | -6.7    | 10.7    | 4.1                   |

Source: Pakistani authorities; and own calculations.

1/ Defined as the deviation of the large-scale manufacturing index from its trend in percent of the trend.

Table 3. Pakistan: Test of Nonstationarity of Core Variables

|                                    | Level  | First<br>Difference | Critical<br>Value 1/ |
|------------------------------------|--------|---------------------|----------------------|
| Augmented Dickey Fuller Test       |        |                     |                      |
| CPI 2/                             | 1.844  | -6.674              | -2.900               |
| Inflation 2/                       | -2.255 | -2.010              | -2.900               |
| Broad money 2/                     | -1.872 | -1.964              | -2.900               |
| Credit to the private sector 2/    | -4.214 |                     | -2.900               |
| Large scale manufacturing index 2/ | -4.296 |                     | -2.900               |
| Output gap 2/                      | -8.582 |                     | -2.900               |
| Phillips Perron Test               |        |                     |                      |
| CPI 2/                             | 1.715  | -6.674              | -2.900               |
| Inflation 3/                       | -0.510 | -2.328              | -1.945               |
| Broad money 3/                     | -0.164 | -1.946              | -1.945               |
| Credit to the private sector 3/    | 0.651  | -1.555              | -1.945               |
| Large scale manufacturing index 2/ | -4.422 |                     | -2.902               |
| Output gap 2/                      | -8.608 |                     | -2.902               |

Source: Pakistani authorities; and own calculations.

1/ Critical value at the 5 percent significant level as provided by Eviews.

2/ Model includes intercept.

3/ Model without intercept.

Table 4. Pakistan: Regression Results for a Money Demand Function with Annual Data

| Dependent variable                 | Log CPI inflation  |                    |
|------------------------------------|--------------------|--------------------|
| Sample                             | 1975 to 2004       |                    |
| Observations                       |                    | 30                 |
| Adjusted R-squared                 |                    | 0.99               |
| Durbin-Watson                      |                    | 0.43               |
| F-statistic                        |                    | 1,125.68           |
| Engle-Granger test 1/<br>Statistic |                    | -1.76              |
| Critical value                     |                    | -3.74              |
|                                    | <u>Coefficient</u> | <u>t-Statistic</u> |
| Constant                           | -3.46              | -8.277996          |
| Log M2                             | 0.63               | 6.065496           |
| Log Real GDP                       | -0.18              | -0.63925           |

Sources: International Financial Statistics; and own calculations.

1/ Test for cointegration based on regression residuals. See Davidson/MacKinnon (1993).

Table 5. Pakistan: Regression Results for a Money Demand Function with Monthly Data

| Dependent variable                 | Log CPI inflation  |                    |
|------------------------------------|--------------------|--------------------|
| Sample                             | 1995:04 to 2004:07 |                    |
| Observations                       |                    | 112                |
| Adjusted R-squared                 |                    | 0.98               |
| Durbin-Watson                      |                    | 0.17               |
| F-statistic                        |                    | 2,336.55           |
| Engle-Granger test 1/<br>Statistic |                    | -3.53              |
| Critical value                     |                    | -3.74              |
|                                    | <u>Coefficient</u> | <u>t-Statistic</u> |
| Constant                           | -2.44              | -23.27             |
| Log M2                             | 0.91               | 33.43              |
| Log Manufacturing Index            | -1.16              | -17.49             |

Sources: International Financial Statistics; and own calculations.

1/ Test for cointegration based on regression residuals. See Davidson/MacKinnon (1993).

Table 6. Pakistan: Forecast Quality of Different ARIMA(p,1,q) Specifications

| Model                            | p  | q  | Adj. R-Squared | F-Statistic | Akaike Information Criterion | Schwarz Information Criterion | Root Mean Squared Error | Mean Absolute Error | Mean Absolute Percentage Error | Theil In-equality Coef. |
|----------------------------------|----|----|----------------|-------------|------------------------------|-------------------------------|-------------------------|---------------------|--------------------------------|-------------------------|
| Without Islamic Calendar Dummies |    |    |                |             |                              |                               |                         |                     |                                |                         |
| 1                                | 1  | 1  | 0.822          | 176.277     | -1.790                       | -1.699                        | 0.095                   | 0.071               | 113.608                        | 0.218                   |
| 2                                | 2  | 2  | 0.829          | 92.082      | -1.818                       | -1.665                        | 0.091                   | 0.066               | 107.951                        | 0.210                   |
| 3                                | 3  | 3  | 0.839          | 65.217      | -1.863                       | -1.647                        | 0.087                   | 0.064               | 116.932                        | 0.201                   |
| 4                                | 4  | 4  | 0.834          | 46.908      | -1.811                       | -1.531                        | 0.087                   | 0.065               | 123.758                        | 0.199                   |
| 5                                | 5  | 5  | 0.865          | 47.139      | -1.993                       | -1.648                        | 0.077                   | 0.062               | 128.325                        | 0.176                   |
| 6                                | 6  | 6  | 0.875          | 42.271      | -2.035                       | -1.624                        | 0.073                   | 0.060               | 120.543                        | 0.166                   |
| 7                                | 7  | 7  | 0.882          | 38.487      | -2.061                       | -1.583                        | 0.070                   | 0.054               | 115.497                        | 0.158                   |
| 8                                | 8  | 8  | 0.857          | 26.882      | -1.833                       | -1.287                        | 0.076                   | 0.060               | 107.661                        | 0.170                   |
| 9                                | 9  | 9  | 0.919          | 43.653      | -2.374                       | -1.759                        | 0.056                   | 0.045               | 81.866                         | 0.124                   |
| 10                               | 10 | 10 | 0.857          | 21.002      | -1.775                       | -1.089                        | 0.073                   | 0.057               | 94.052                         | 0.163                   |
| 11                               | 11 | 11 | 0.944          | 51.161      | -2.680                       | -1.923                        | 0.045                   | 0.036               | 83.542                         | 0.097                   |
| 12                               | 11 | 11 | 0.870          | 19.884      | -1.839                       | -1.043                        | 0.067                   | 0.054               | 92.857                         | 0.148                   |
| 6                                | 1  | 1  | 0.821          | 47.619      | -1.738                       | -1.485                        | 0.091                   | 0.068               | 114.317                        | 0.209                   |
| 6                                | 0  | 0  | 0.082          | 56.410      | -1.766                       | -1.544                        | 0.091                   | 0.068               | 113.866                        | 0.209                   |
| 5                                | 1  | 1  | 0.832          | 60.608      | -1.824                       | -1.604                        | 0.088                   | 0.066               | 115.992                        | 0.204                   |
| 5                                | 0  | 0  | 0.822          | 67.484      | -1.775                       | -1.587                        | 0.092                   | 0.069               | 115.885                        | 0.212                   |
| With Islamic Calendar Dummies 1/ |    |    |                |             |                              |                               |                         |                     |                                |                         |
| 11                               | 11 | 11 | 0.842          | 14.486      | -1.624                       | -0.735                        | 0.072                   | 0.056               | 97.380                         | 0.160                   |
| 5                                | 1  | 1  | 0.831          | 36.529      | -1.771                       | -1.426                        | 0.086                   | 0.064               | 118.338                        | 0.197                   |

Sources: International Financial Statistics; and own calculations.

1/ Dummies taken from Riazuddin and Khan (2002).

Table 7. Pakistan: Estimation Results for the ARIMA(5,1,1)

| Dependent variable<br>Sample | Log CPI inflation<br>June 1998 to December 2004 |             | Log CPI inflation<br>June 1998 to December 2004 |             |
|------------------------------|---|-------------|---|-------------|
|                              | Coefficient                                     | t-Statistic | Coefficient                                     | t-Statistic |
| Observations                 |   | 72          |   | 72          |
| Adjusted R-squared           |   | 0.83        |   | 0.83        |
| Durbin-Watson                |   | 1.99        |   | 1.99        |
| F-statistic                  |   | 60.61       |   | 36.53       |
| Constant                     | 0.00  | 0.01        | -0.02   | -0.23       |
| AR(1)                        | 0.09  | 0.73        | 0.12  | 0.91        |
| AR(2)                        | 0.80  | 6.22        | 0.79  | 6.05        |
| AR(3)                        | 0.27  | 1.72        | 0.27  | 1.73        |
| AR(4)                        | -0.22   | -1.73       | -0.23   | -1.79       |
| AR(5)                        | -0.24   | -1.80       | -0.26   | -1.92       |
| MA(1)                        | 0.96  | 42.90       | 0.96  | 39.17       |
| Dummy for<br>Muharram        |   |             | 0.03  | 0.66        |
| Dummy for<br>Ramashan        |   |             | 0.02  | 0.58        |
| Dummy for Shawal             |   |             | 0.08  | 1.88        |
| Dummy for Thul<br>Hujja      |   |             | 0.00  | -0.01       |

Sources: International Financial Statistics; and own calculations.

Table 8. Pakistan: VAR Regression Results

|                       | Inflation 1/ |         | Real interest rate 2/ |         | Output gap |         |
|-----------------------|--------------|---------|-----------------------|---------|------------|---------|
|                       | Coef.        | t-stat. | Coef.                 | t-stat. | Coef.      | t-stat. |
| Constant              | -0.0003      | -0.8169 | -0.0041               | -1.4852 | -0.0061    | -0.9759 |
| Inflation 1/          |              |         |                       |         |            |         |
| Lag 1                 | 0.5214       | 1.9480  | -0.0113               | -0.0949 | -0.0004    | -0.0304 |
| Lag 2                 | 0.1801       | 0.5766  | -0.1692               | -1.2216 | -0.0136    | -0.8003 |
| Lag 3                 | -0.1076      | -0.4780 | 0.1871                | 1.8754  | 0.0020     | 0.1605  |
| Real interest rate 2/ |              |         |                       |         |            |         |
| Lag 1                 | -0.6722      | -1.6405 | 0.6308                | 3.4724  | 0.0086     | 0.3888  |
| Lag 2                 | 0.1086       | 0.2453  | -0.0169               | -0.0863 | -0.0326    | -1.3566 |
| Lag 3                 | 0.1000       | 0.2456  | 0.2431                | 1.3460  | -0.0030    | -0.1360 |
| Output gap            |              |         |                       |         |            |         |
| Lag 1                 | 1.4412       | 0.3830  | 0.5388                | 0.3229  | 0.2053     | 1.0059  |
| Lag 2                 | 8.9753       | 2.5371  | -1.2028               | -0.7669 | -0.3285    | -1.7127 |
| Lag 3                 | 5.9956       | 1.3974  | 2.1870                | 1.1497  | 0.1175     | 0.5049  |
| Adjusted R-square     | 0.75         |         | 0.80                  |         | -0.05      |         |
| F Statistic           | 11.62        |         | 15.12                 |         | 0.82       |         |

Sources: Pakistani authorities; and own estimates.

1/ Annual average inflation.

2/ The real interest rate is defined as the nominal 3-month t-bill rate less expected inflation, where inflation expectations are based on an ARMA model.



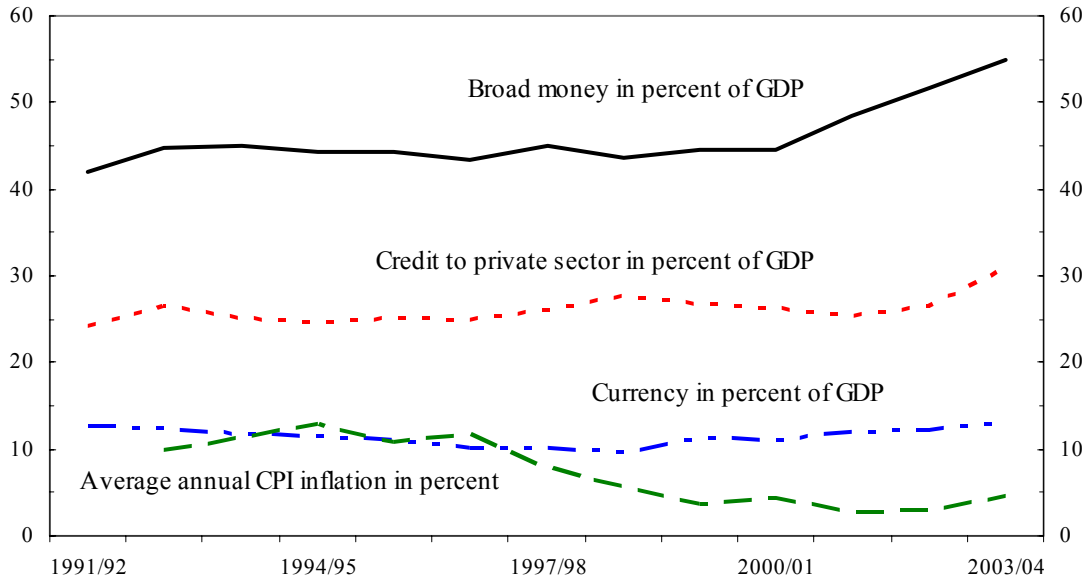
Table 9. Pakistan: Leading Indicators Model Regression Results

|   | Model 1     |             | Model 2     |             | Model 3     |             | Model 4     |             |
|---|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
|   | Coefficient | t-Statistic | Coefficient | t-Statistic | Coefficient | t-Statistic | Coefficient | t-Statistic |
| Observations  | 73          |             | 72          |             | 72          |             | 76          |             |
| Adjusted R-squared                                      | 0.995       |             | 0.996       |             | 0.996       |             | 0.996       |             |
| F-statistic   | 2,555.1     |             | 881.6       |             | 3,560.4     |             | 3,412.3     |             |
| Akaike Information Criterion                            | -1.935      |             | -1.967      |             | -2.136      |             | -1.913      |             |
| Schwarz Information Criterion                           | -1.716      |             | -1.303      |             | -1.947      |             | -1.729      |             |
| Root Mean Squared Error                                 | 0.397       |             | 0.358       |             | 0.388       |             | 1.409       |             |
| Mean Absolute Error                                     | 0.350       |             | 0.280       |             | 0.358       |             | 1.259       |             |
| Mean Absolute Percentage Error                          | 5.662       |             | 4.300       |             | 5.834       |             | 18.941      |             |
| Constant  | 0.111       | 2.813       | -0.069      | -0.585      | -0.182      | -2.638      | 0.086       | 2.082       |
| Inflation   |             |             |             |             |             |             |             |             |
| Lagged 1 month  | 1.772       | 14.949      | 1.680       | 10.272      | 1.508       | 16.025      | 1.910       | 37.363      |
| Lagged 2 months   | -0.760      | -4.629      | -0.843      | -2.876      | -0.651      | -8.471      | -0.935      | -18.128     |
| Lagged 3 months   |             |             | 0.111       | 0.346       |             |             |             |             |
| Lagged 4 months   |             |             | -0.231      | -0.710      |             |             |             |             |
| Lagged 5 months   | -0.194      | -1.189      | 0.126       | 0.429       |             |             |             |             |
| Lagged 6 months   | 0.144       | 1.266       | 0.024       | 0.182       |             |             |             |             |
| Private sector credit growth                            |             |             |             |             |             |             |             |             |
| Lagged 6 months   |             |             | 0.086       | 1.623       |             |             |             |             |
| Lagged 7 months   |             |             | -0.176      | -1.507      |             |             |             |             |
| Lagged 8 months   |             |             | 0.087       | 0.689       |             |             |             |             |
| Lagged 9 months   |             |             | 0.052       | 0.412       |             |             |             |             |
| Lagged 10 months  |             |             | -0.068      | -0.532      |             |             |             |             |
| Lagged 11 months  | 0.042       | 2.711       | 0.020       | 0.162       |             |             |             |             |
| Lagged 12 months  | -0.038      | -2.444      | 0.036       | 0.547       | 0.041       | 4.991       |             |             |
| Broad money growth                                      |             |             |             |             |             |             |             |             |
| Lagged 6 months   |             |             | -0.157      | -2.169      |             |             | -0.114      | -2.270      |
| Lagged 7 months   |             |             | 0.407       | 3.164       | 0.145       | 3.775       | 0.210       | 2.211       |
| Lagged 8 months   |             |             | -0.262      | -1.847      | -0.116      | -3.392      | -0.094      | -1.949      |
| Lagged 9 months   |             |             | 0.028       | 0.188       |             |             |             |             |
| Lagged 10 months  |             |             | 0.074       | 0.522       |             |             |             |             |
| Lagged 11 months  |             |             | -0.072      | -0.558      |             |             |             |             |
| Lagged 12 months  |             |             | 0.001       | 0.017       |             |             |             |             |
| Long run coefficient 1/<br>Private sector credit growth | 10.00       |             | 3.53        |             | 3.47        |             |             |             |
| Broad money growth                                      |             |             | 7.12        |             | 4.85        |             | 13.99       |             |

Sources: Pakistani authorities; and own calculations.

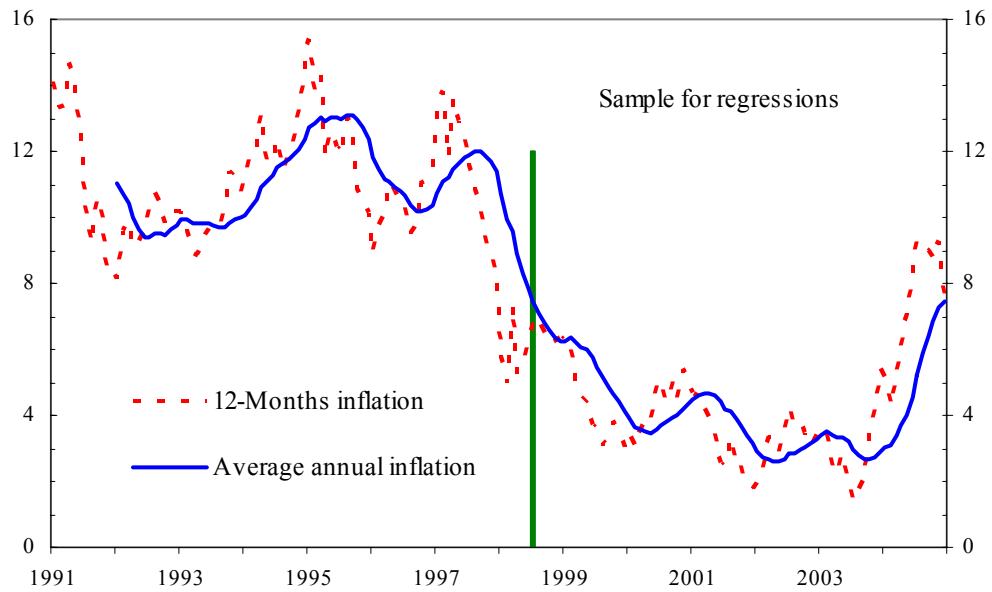
1/ Calculated as  $(1 - \text{sum of coefficients on inflation}) / (\text{sum of coefficients on regressor})$ .

Figure 1. Pakistan: Monetary Developments, 1991/92–2003/04



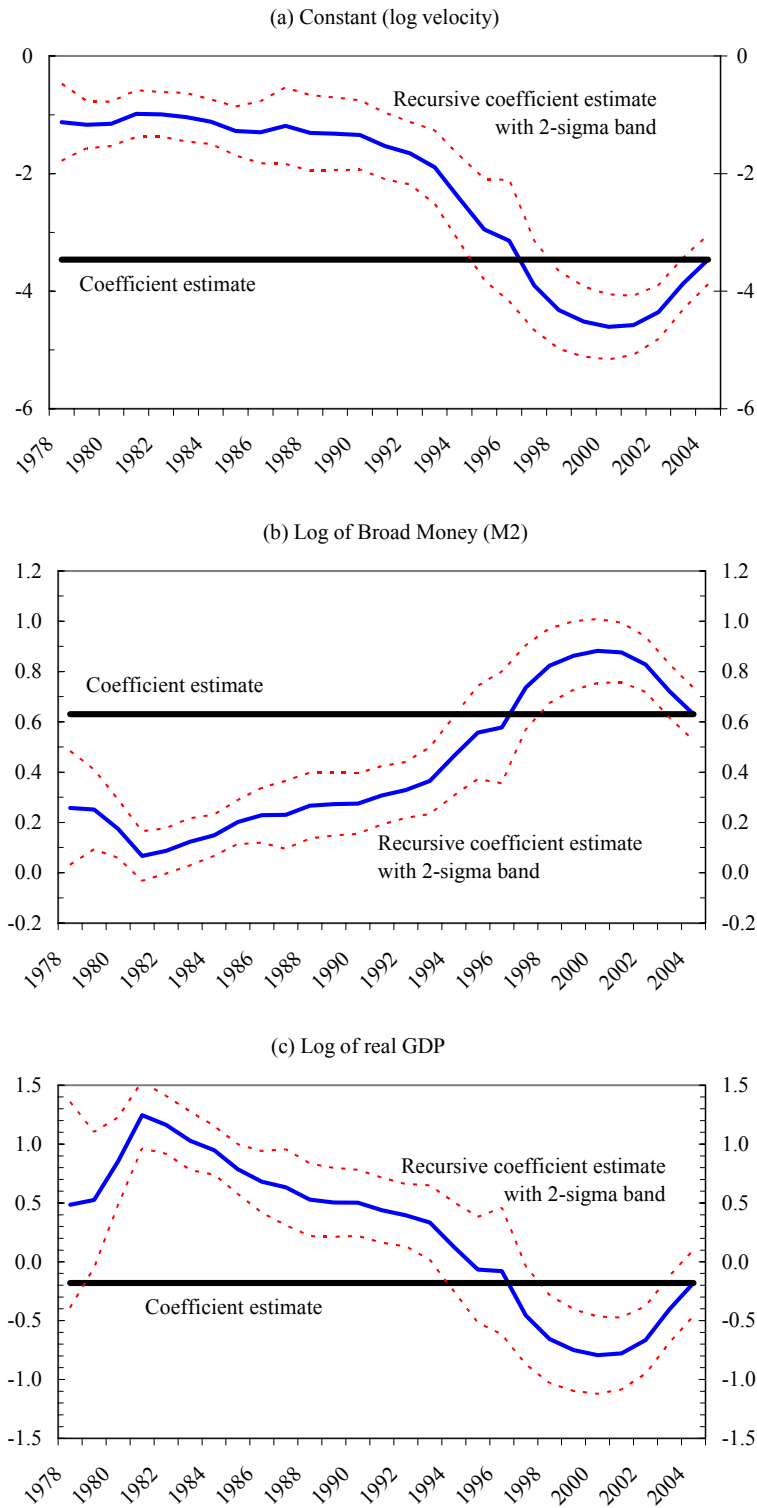
Sources: Pakistani authorities; and own calculations.

Figure 2. Pakistan: CPI Inflation, 1991–2003  
(In percent)



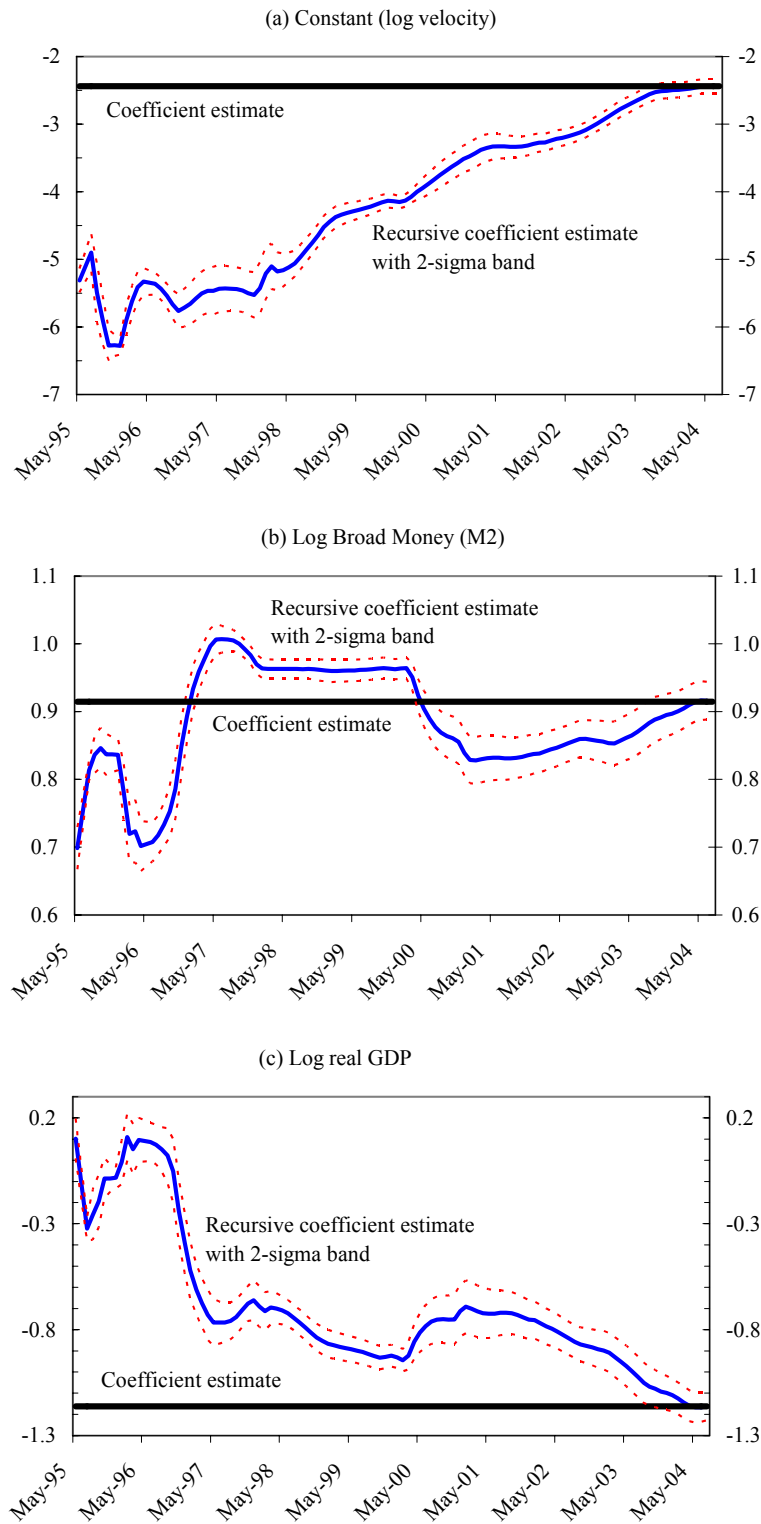
Sources: Pakistani authorities; and own calculations.

Figure 3. Pakistan: Parameter Instability in the Money Demand Equation with Annual Data, 1978–2004



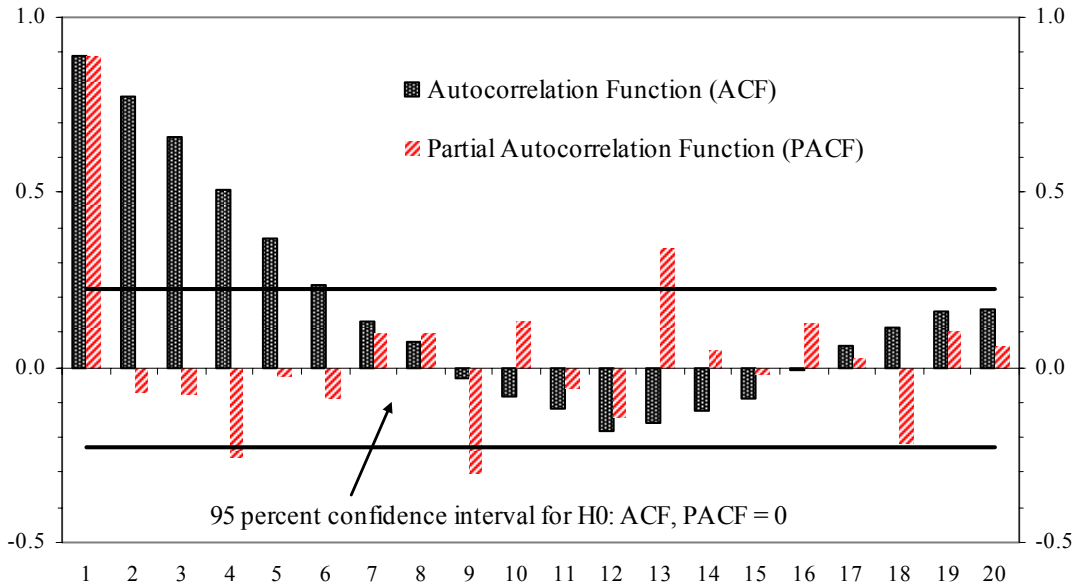
Sources: Pakistani authorities; and own calculations.

Figure 4. Pakistani: Parameter Instability in the Money Demand Equation with Monthly Data, 1995–2004



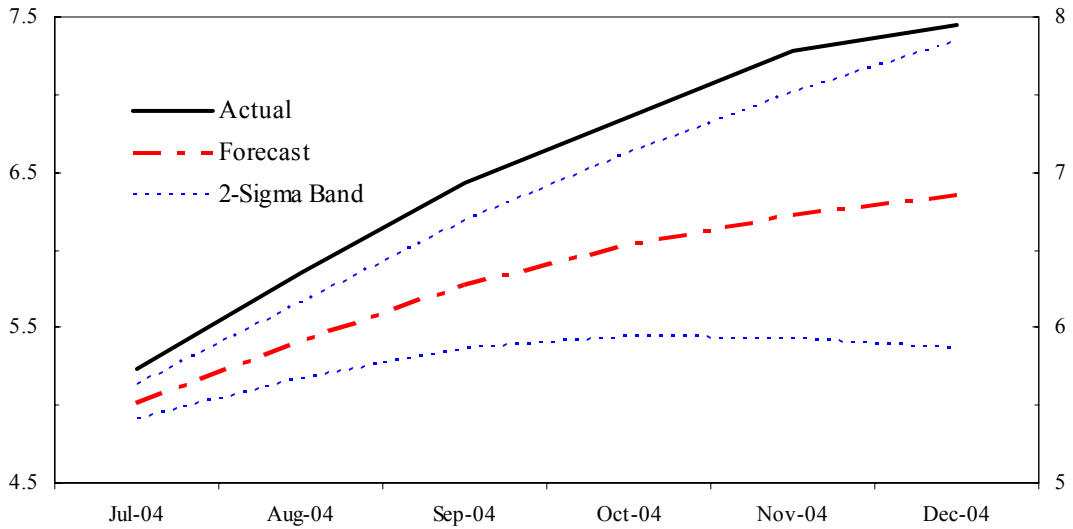
Sources: Pakistani authorities; and own calculations.

Figure 5. Pakistan: Autocorrelation and Partial Autocorrelation Functions



Sources: Pakistani authorities; and own calculations.

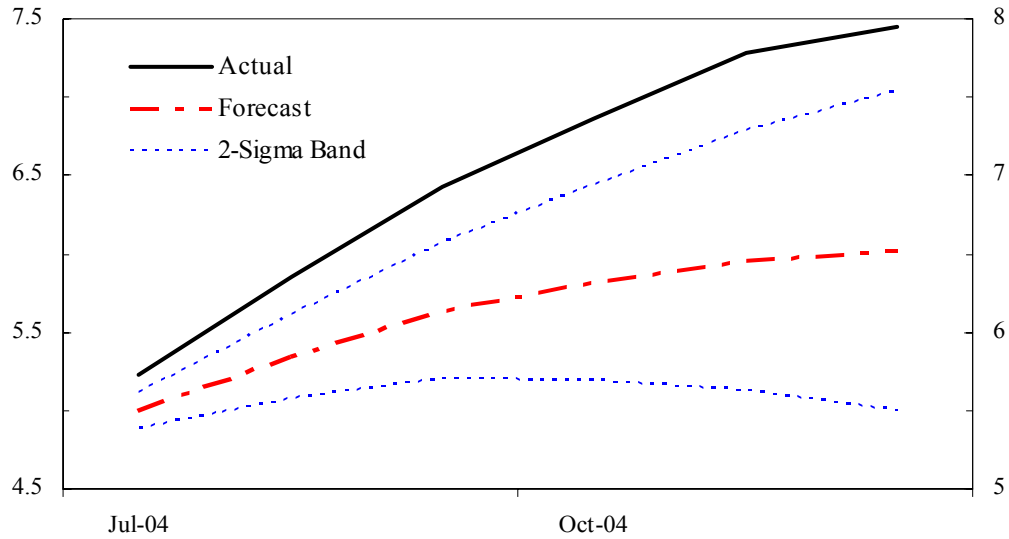
Figure 6. Pakistan: ARIMA(5,1,1)—Ex-post Forecast, Jul–Dec. 2004 1/



Sources: Pakistani authorities; and own projections.

1/ Forecast based on model for reduced sample through June 2004.

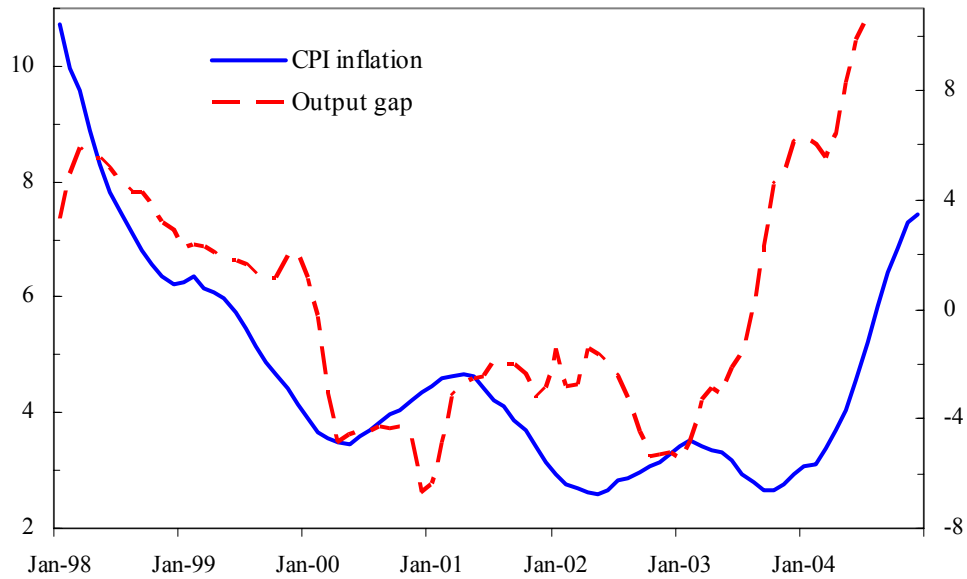
Figure 7. Pakistan: ARIMA(5,1,1) with Islamic Calendar Dummies—  
Ex-post Forecast, Jul.–Oct. 2004 1/



Sources: Pakistani authorities; and own projections.

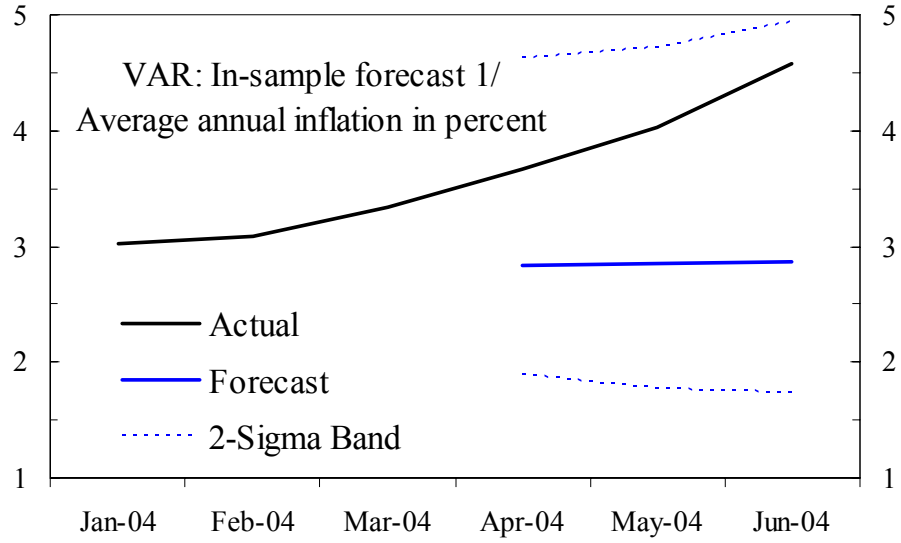
1/ Forecast based on model for reduced sample through June 2004.

Figure 8. Pakistan: The Output Gap—Inflation Link, 1998–2004



Sources: Pakistani authorities; and own calculations.

Figure 9. Pakistan: VAR Model—Ex-post Forecast, Jan.–Jun. 2004 1/

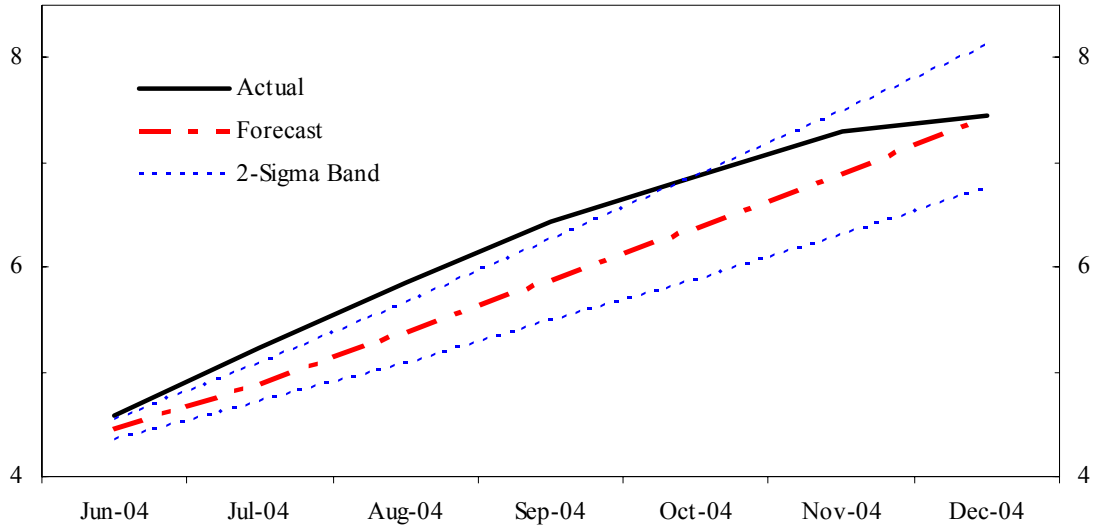


Source: National authorities; and Fund staff calculations.

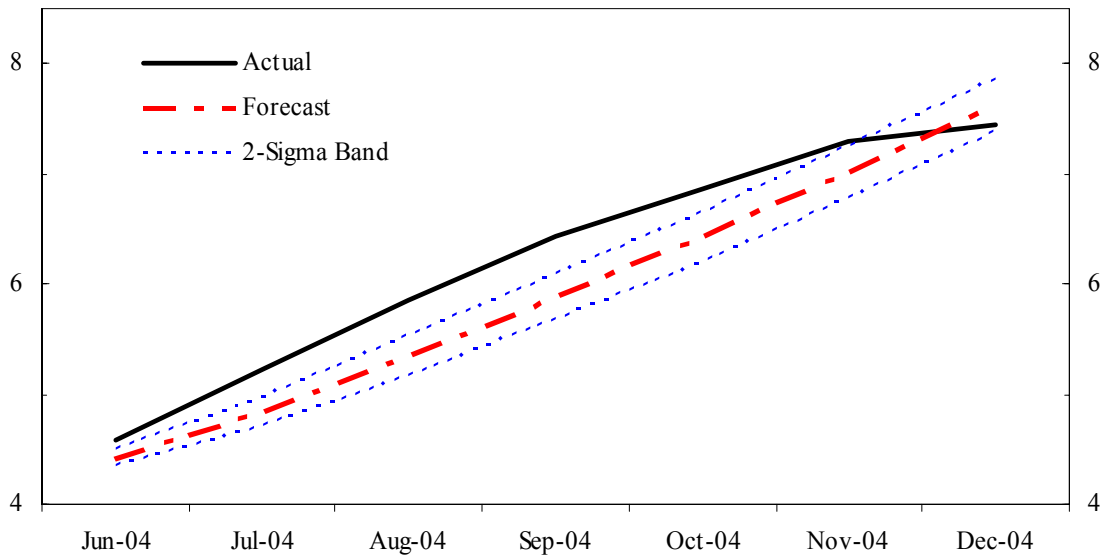
1/ Forecast based on model for reduced sample through March 2004.

Figure 10. Pakistan: Leading Indicator Models—Ex-post Forecasts, Jun.–Dec. 2004 1/

(a) Based on Model 1 (Private Sector Credit Growth)



(b) Based on Model 3 (Broad Money and Private Sector Credit Growth)

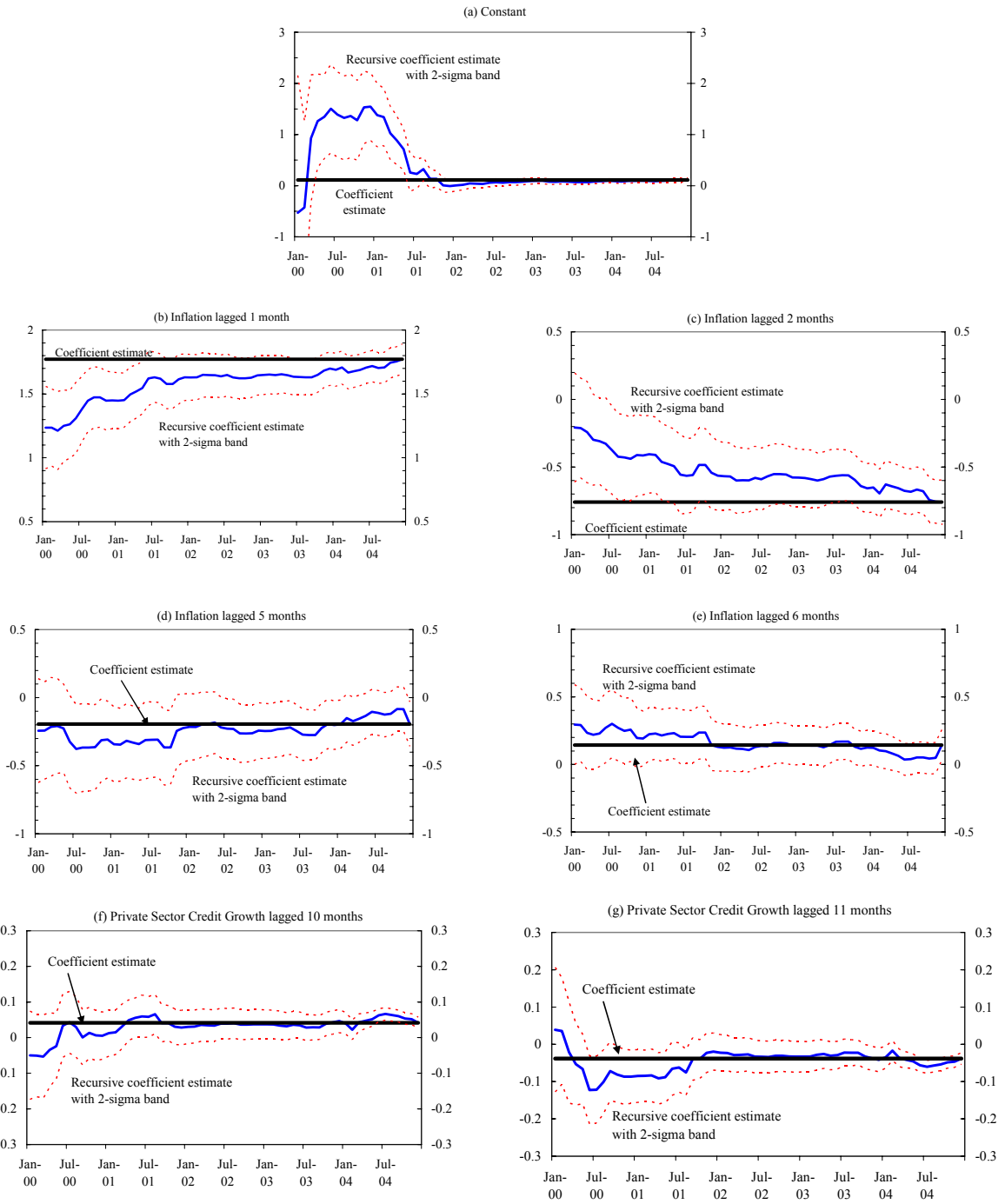


Sources: Pakistani authorities; and own calculations.

1/ Forecast based on model for reduced sample through May 2004.

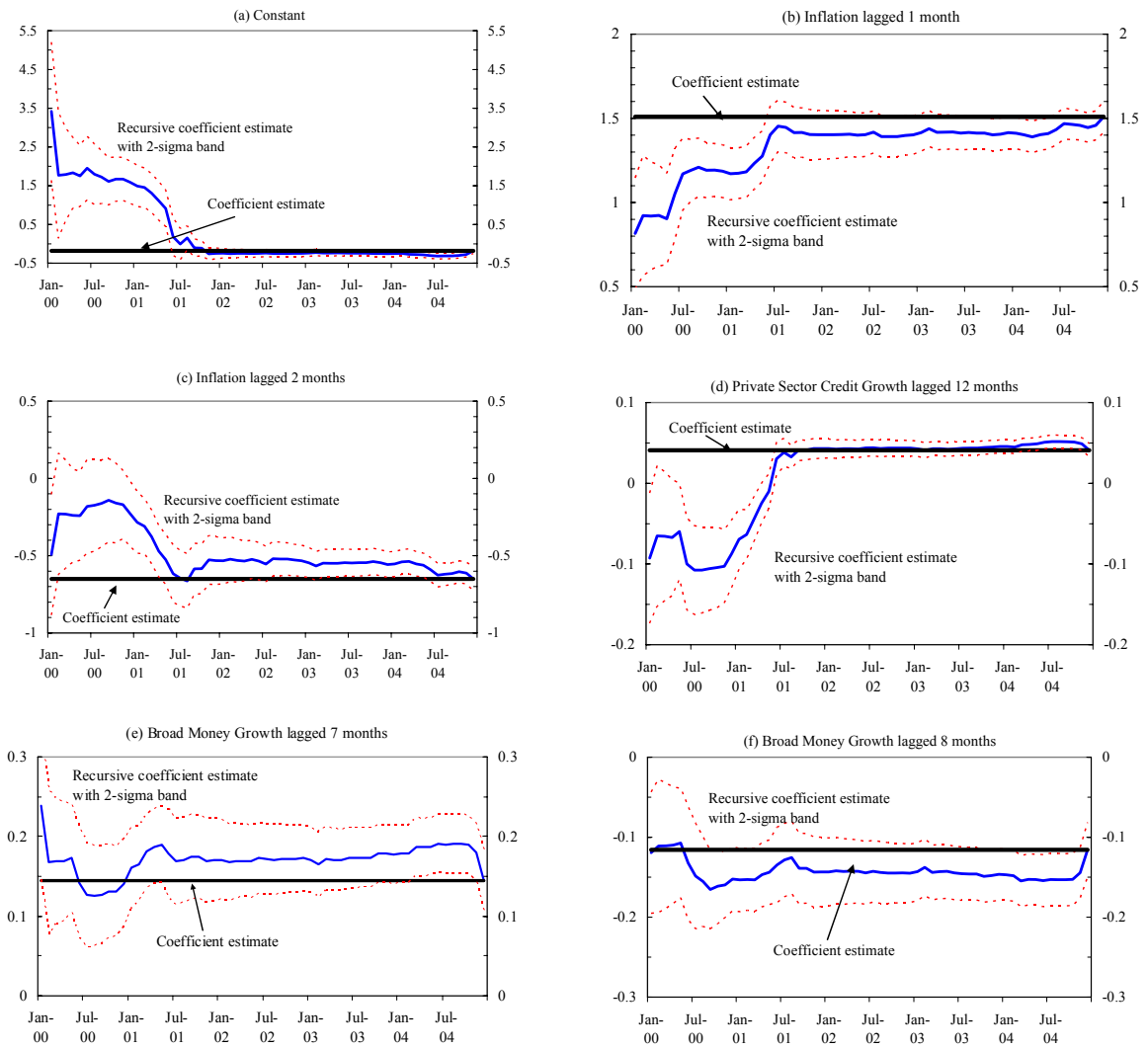


Figure 11. Pakistan: Parameter Stability for Leading Indicators Model 1, 2000–04



Sources: Pakistani authorities; and own calculations.

Figure 12. Pakistan: Parameter Stability for Leading Indicators Model 3, 2000–04



Source: Pakistani authorities; and own calculations.

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