



WP/06/46

# IMF Working Paper

---

## How Different Is the Cyclical Behavior of Home Production Across Countries?

*William Blankenau and M. Ayhan Kose*



**IMF Working Paper**

Research Department

**How Different Is the Cyclical Behavior of Home Production Across Countries?**

Prepared by William Blankenau and M. Ayhan Kose<sup>1</sup>

Authorized for distribution by Eswar Prasad

February 2006

**Abstract**

**This Working Paper should not be reported as representing the views of the IMF.**

The views expressed in this Working Paper are those of the author(s) and do not necessarily represent those of the IMF or IMF policy. Working Papers describe research in progress by the author(s) and are published to elicit comments and to further debate.

This paper studies stylized business cycle properties of household production in four industrialized countries (Canada, the United States, Germany, and Japan). We employ a dynamic small open economy business cycle model that incorporates a household production sector. We use the model to generate data on home output, hours worked in the home sector, and hours spent on leisure. We find that in each country, home output is more volatile than market output while home sector hours are about as volatile as those in the market sector. In each country, leisure is the least volatile series. Leisure hours and home hours are countercyclical in all countries, and home output is not highly correlated with market output. Home sector variables are generally less persistent than market variables, and cross-country correlations related to home production tend to be lower than those related to market production. These findings demonstrate that despite some well-known structural differences in labor markets, the cyclical features of home sector variables are similar across the countries we consider.

JEL Classification Numbers: F40, E32, J22

Keywords: Keywords: Business cycles, home (non-market), production, general equilibrium

Author(s) E-Mail Address: [blankenw@ksu.edu](mailto:blankenw@ksu.edu); [akose@imf.org](mailto:akose@imf.org)

---

<sup>1</sup> A preliminary version of this paper was presented at the Society for Computational Economics Meetings at Yale University. We would like to thank an anonymous referee, Ken Beauchemin, Beth Ingram, Robert Kollmann, Kei-Mu Yi, and seminar participants for useful suggestions. Kulaya Tantitemit provided superb research assistance. This paper is forthcoming in *Macroeconomic Dynamics*.

	Contents	Page
I.	Introduction.....	3
II.	The Model.....	5
III.	Data .....	8
IV.	Parameter Calibration .....	9
V.	Results.....	10
	A. Time Series Behavior.....	10
	B. Stylized Features of Business Cycle Dynamics .....	11
	C. Sensitivity Analysis.....	17
VI.	Conclusion .....	18
Figures		
1.	Hours .....	20
2.	Output and Consumption .....	21
3.	Home Consumption .....	22
Tables		
1.	Relative Volatility.....	23
2.	Persistence.....	24
3.	Comovement.....	25
4.	Driving Processes.....	26
5.	Cross-Country Correlations .....	27
	References.....	28

## I. INTRODUCTION

A large part of economic activity occurs in the home. Empirical studies suggest that the value of home (household) production is between 40 and 50 percent of measured GNP in most industrialized countries.<sup>2</sup> Because of its quantitative importance, an understanding of fluctuations in household production strengthens our understanding of aggregate economic fluctuations. Recognizing this, researchers have incorporated household production into stochastic dynamic business cycle models. This innovation has yielded models that outperform their predecessors in terms of matching several business cycle features. For example, Greenwood, Rogerson, and Wright (GRW, 1995) find that introducing a household production sector into an otherwise standard closed-economy business cycle model improves significantly the ability of the model to explain both the volatility of major macroeconomic aggregates and their comovements.<sup>3</sup>

Motivated in part by such successes, the application of stochastic dynamic home production models has been widespread. These models have proliferated despite an obvious weakness; time series on home production do not exist.<sup>4</sup> To circumvent the scarcity of relevant data, most researchers employ simplifying assumptions to identify the home productivity shocks in a parameterized dynamic stochastic model. Following the standard business cycle methodology, they then solve and simulate the model to generate artificial data related to market production and home production. For the market series, they are able to evaluate whether the moments of the artificial data are consistent with those of observed data. For the home sector, no observed data are available for a similar evaluation. Researchers report the moments for home sector variables and provide intuition regarding these moments. However, they cannot gauge the extent to which the model generates home sector data consistent with actual economies.

---

<sup>2</sup> See Eisner (1988) and Bonke (1992) for empirical evidence on this. Furthermore, Juster and Stafford (1991) find that a typical married U.S. couple spends 25 percent of their time working at home while allocating 33 percent of their time to market activities. Bonke (1995) finds that women allocate as much as 57 percent and men as much as 21 percent of their time to home production. Greenwood, Rogerson, and Wright (1995) document that investment in household capital is larger than in market capital.

<sup>3</sup> See also Benhabib, Rogerson, and Wright (1991); Greenwood and Hercowitz (1991); Baxter and Jermann (1999); and Wrase (2001). Busato and Chiarini (2004) also analyze the role of home production activity in explaining business cycles.

<sup>4</sup> McGrattan, Rogerson, and Wright (1997) evaluate the impact of fiscal policy; Canova and Ubide (1997) study business cycle transmission across countries; and Parente, Rogerson, and Wright (1999) examine the sources of differences in the standard of living across countries. It is possible to obtain spotty data related to home production activities collected through surveys and time-use diaries (see Juster and Stafford (1991)). Gronau and Hamermesh (2006) examine the U.S. and Israeli household data on expenditures of time and goods to analyze how education and age affect the goods intensity of household production.

Ingram, Kocherlakota, and Savin (IKS, 1997) develop a complementary approach to deal with the problem of unobservable data.<sup>5</sup> While the two approaches have similarities, the IKS approach is complementary to the standard approach in that it does not rely on simplifying assumptions to identify home sector productivity shocks. Instead IKS use “theory for measurement.” Specifically, they use the Euler equations from a dynamic stochastic model with a home production sector to derive a mapping from observable market data to unobservable home sector data. They then calibrate the model to the U.S. economy and use the U.S. data on market hours, market consumption, and output to derive series for home output, hours spent in home production, and hours spent at leisure.

In this paper, we use the IKS approach to address several open questions regarding the business cycle properties of the home sector. The first is whether there are similarities in these properties across similar economies. To address this, we document the stylized business cycle features of home production activities in industrialized countries. While the Group of Seven (G-7) countries would be the most appropriate set to consider, data limitations require that we restrict attention to Canada, the United States, Germany, and Japan. These economies are similar, of course, in levels of industrialization and have broadly similar business cycle features in observable data. However, there are some well-known structural differences in their labor markets that might lead to different home sector behavior.<sup>6</sup>

Our results suggest that despite these differences, there are some important similarities in the cyclical properties of home sector variables across the countries we consider. For example, we find that home production is more volatile than market production, while the volatility of hours spent in home production is close to that of market hours. Leisure is much less volatile than any other series. In addition, home production variables are less persistent than market variables. Leisure hours and home hours are both countercyclical, while home production has no strong correlation with market production. It may be surprising to find such regularities in these features, given that there are some differences in the functioning of labor markets in these countries. However, while the model does not take the labor market differences into account directly, the observable data from each country should reflect these differences.

---

<sup>5</sup> This approach is not unique to IKS and has recently been widely used in different contexts. For example, employing this approach, IKS (1994a, 1994b) back out the productivity shocks and examine their roles in driving business cycles; Baxter and King (1998) back out the realizations of productivity and preference shocks, Smith and Zin (1997) generate realizations of output, consumption, and employment; Blankenau, Kose, and Yi (2001) back out the world real interest rate series; and Beauchemin (2000) generates public capital series. IKS (1994a, 1994b) also apply this methodology to derive productivity shocks.

<sup>6</sup> See Siebert (1997) for a study of structural differences in the labor markets of nine member countries of the Organization for Economic Co-operation and Development. Genay and Loungani (1997) study the similarities and differences in the cyclical dynamics of labor markets in the United States and Japan. Bertola and Rogerson (1997) analyze the differences in labor markets in Europe and the United States and emphasize the importance of these in explaining the dynamics of unemployment.

Furthermore, all four countries are well-developed market economies, and similarities in their cyclical responses to shocks could partly reflect this.

The second question we address is whether cyclical fluctuations in the home sector are related across countries. Since there is no other study that compares home sector variables across countries, we provide the first evidence regarding this question. Since home sector output is not tradable, one would expect cross-country correlations for home series to be lower than those for market series. We find that this hypothesis holds in nearly every case. For home consumption, cross-country correlations are mostly negative.

Another question is whether home production models are able to replicate business cycle features of household production. This question cannot be answered directly, since the actual series are unobservable. However, we can gauge the extent to which the business cycle properties of home sector data derived in the standard approach are consistent with our data. Since the IKS approach generates series that are informed by the data, this provides an appropriate comparison. We address this question in two ways. First, we consider whether the business cycle properties that we found to be robust across countries arise in the home series generated by other studies. The results suggest that there is considerable consistency between the findings in other studies and the stylized facts we document here. We then consider whether the assumptions used by other studies to identify the home sector shocks are consistent with the moments of our derived shocks. We provide empirical support for some of the assumptions made by the other studies to identify shocks in household production; the processes that they assume are largely consistent with those that we derive. There are some differences, of course, and these are outlined in the text.

The rest of the paper is organized as follows. In Section II, we present the model and our empirical methodology. In Sections III and IV, we provide information about the data sources and model calibration, respectively. Section V discusses the results. A brief conclusion and a summary of the results are in Section VI.

## II. THE MODEL

Our model is a small open economy version of Benhabib, Rogerson, and Wright (BRW, 1991). There is an infinitely lived representative agent, who derives utility from home produced goods ( $c_{nt}$ ), market produced ( $c_{mt}$ ) goods, and leisure ( $l_t$ ). The agent maximizes the following lifetime utility function

$$E_0 \left( \sum_{t=1}^{\infty} \beta^t \left( (1 - \gamma_l) \ln \left[ \gamma_m c_{mt}^\rho + (1 - \gamma_m) c_{nt}^\rho \right]^{1/\rho} + \gamma_l \ln(l_t) \right) \right).$$

We restrict  $\beta, \gamma_l, \gamma_m \in [0, 1]$  and  $\rho \leq 1$ . The period utility function, then, is Cobb-Douglas in leisure and a CES combination of  $c_{mt}$  and  $c_{nt}$ .<sup>7</sup> Here  $(1 - \rho)^{-1}$  is the elasticity of substitution across the consumption goods and  $\gamma_m$  is the share of market consumption in total consumption.

The representative agent is endowed in each period with one unit of time which is allocated across production of market goods, production of home goods, and leisure. In the market sector, the agent combines market labor with market capital to produce a final market good. Similarly, in the home (or nonmarket) sector, home labor and capital are combined to produce a final home good. In each sector, goods are produced according to a Cobb-Douglas technology. Let  $h_{mt}$ ,  $h_{nt}$ ,  $k_{mt}$ , and  $k_{nt}$  be the labor and capital employed in the market and home sectors and let  $y_{mt}$  and  $y_{nt}$  be the output in these sectors, respectively. The sector production functions are:

$$\begin{aligned} y_{mt} &= A_{mt} k_{mt}^{\alpha_m} h_{mt}^{(1-\alpha_m)} \\ y_{nt} &= A_{nt} k_{nt}^{\alpha_n} h_{nt}^{(1-\alpha_n)}. \end{aligned}$$

$A_{mt}$  and  $A_{nt}$  are sector specific productivity shocks. The parameters  $\alpha_m$  and  $\alpha_n$  denote capital share in the market and home sectors respectively, and are between zero and one. Market hours, nonmarket hours and leisure are linked by the requirement:

$$h_{mt} + h_{nt} + l_t = 1. \quad (1)$$

The agent can buy and sell foreign financial assets, which are one-period risk-free bonds, in world financial markets. As in BRW, we further distinguish the sectors by requiring that output in the home sector be consumed only and that all home consumption be produced in the home sector. In contrast, market output can be consumed, invested, or exported in exchange for foreign assets. Specifically, we require:

$$\begin{aligned} c_{nt} &= y_{nt} \\ c_{mt} &= y_{mt} - i_t - nx_t \\ nx_t &= A_{t+1} - (1 + r_t) A_t. \end{aligned} \quad (2)$$

where  $c_{mt}$  and  $c_{nt}$  are market and nonmarket consumption,  $i_t$  is investment,  $nx_t$  is net exports,  $A_t$  is net foreign asset holdings, and  $r_t$  is the world real interest rate. A unit of current investment transforms to a unit of capital in the following period. Capital moves freely across the sectors and depreciates at rate  $\delta$ . Thus,

$$\begin{aligned} k_t &= k_{mt} + k_{nt} \\ k_{t+1} &= i_t + (1 - \delta) k_t. \end{aligned}$$

---

<sup>7</sup> See Kose (2002) for a brief survey about the use of small open economy models in analyzing business cycles. Kim and Kose (2003) discuss the implications of different types of utility and discount factor formulations in these models.



The standard real business cycle approach involves calibrating the model's parameters, specifying forcing processes of the exogenous shocks, and then solving the model. The model's solution is then used to derive the moments of interest and to calculate impulse responses. Rather than produce simulated time series for endogenous variables, we use the observable endogenous variables and the Euler equations to recover the time series of home sector variables. In particular, we exploit the structure imposed by this model to find expressions for the unobservable data series of interest  $(c_{nt}, h_{nt}, y_{nt}, l_{nt})$  in terms of observable data  $(c_{mt}, h_{mt}, y_{mt})$  and the parameters of the model  $(\alpha_m, \alpha_n, \delta, \gamma_m, \gamma_l, \beta, \rho)$ .

Solving for the optimal allocation of consumption across market and home goods and using the constraint that home output and consumption are equal yields the following expression:

$$\left(\frac{c_{nt}}{c_{mt}}\right)^\rho = \frac{\gamma_m}{1-\gamma_m} \frac{1-\alpha_m}{\alpha_m} \frac{y_{mt}}{c_{mt}} \frac{h_{nt}}{c_{nt}}. \quad (3)$$

Solving for the optimal mix of consumption and leisure leads to:

$$\left(\frac{c_{nt}}{c_{mt}}\right)^\rho \frac{1-\gamma_m}{\gamma_m} = (1-\alpha_m) \frac{1-\gamma_l}{\gamma_l} \frac{y_{mt}}{h_{mt}} \frac{l_t}{c_{mt}} - 1. \quad (4)$$

Using equations (1), (3), and (4) to solve for home hours, leisure, and home consumption and functions of observable data gives:

$$l_t = a \frac{\gamma_l}{1-\gamma_l} \left( 1 - h_{mt} \left( 1 - \frac{c_{mt}}{y_{mt}} \frac{1-\alpha_n}{1-\alpha_m} \right) \right) \quad (5)$$

$$h_{nt} = a(1-\alpha_n) \left( 1 - h_{mt} \left( 1 + \frac{c_{mt}}{y_{mt}} \frac{\gamma_l}{1-\gamma_l} \frac{1}{1-\alpha_m} \right) \right) \quad (6)$$

$$c_{nt} = c_{mt} \left( \left( (1-\alpha_m) a \frac{\gamma_m}{1-\gamma_m} \right)^{1/\rho} \left( \frac{1-h_{mt}}{h_{mt}} \frac{y_{mt}}{c_{mt}} - \frac{1}{1-\alpha_m} \frac{\gamma_l}{1-\gamma_l} \right) \right)^{\rho}. \quad (7)$$

where  $a = \frac{1-\gamma_l}{\gamma_l + (1-\alpha_n)(1-\gamma_l)}$ . After calibrating the parameters of the model, these equations

with observed market aggregates can be used to generate series for home hours, leisure, and home consumption.

These expressions are informative about some properties of the derived series. From (5) notice that  $\rho$  and  $\gamma_m$  have no effect on our imputed leisure series. Also  $\gamma_l$  serves only to scale the series upwards and thus will have no effect on the HP-filtered series. The share parameters  $\alpha_n$  and  $\alpha_m$  both scale the series upwards and influence the business cycle

properties. Specifically, these properties will depend parametrically on  $\frac{1-\alpha_n}{1-\alpha_m}$ . Similarly,

from (6) the business cycle properties of home hours will not be affected by the parameters

outside the parenthesis,  $a(1-\alpha_n)$ , as these only scale the magnitude. The parameter combination  $\frac{\gamma_l}{1-\gamma_l} \frac{1}{1-\alpha_m}$  along with the data will determine business cycle properties. From

(7), the business cycle properties of  $c_m$  will depend only on  $\frac{1}{1-\alpha_m} \frac{\gamma_l}{1-\gamma_l}$  and  $\rho$  while

$\left( (1-\alpha_m) a \frac{\gamma_m}{1-\gamma_m} \right)^{1/\rho}$  will scale the imputed value of home consumption.

We use only the conditions for the optimal *intra-temporal* allocation of resources in deriving the mapping from observables to unobservables. As such, changes affecting the *inter-temporal* dynamics of the model do not have any impact on our results. Modifications in the law of motion for the capital stock or foreign assets do not affect the mapping between home sector and market sector variables. In particular, we make no use of the net foreign asset accumulation equation in (2). As our model differs from the closed economy model in IKS primarily through this expression, our mapping mirrors theirs. The only difference is the inclusion of net exports in the expression for market output in our small open economy setting.<sup>8</sup>

### III. DATA

We use seasonally adjusted quarterly values of consumption, investment, and net exports drawn from the IMF's International Financial Statistics (IFS) for the period 1970:1-2003:4 for Canada, Japan, and the United States, and 1970:1-1997:4 for Germany.<sup>9</sup> Consumption ( $c_t$ ) measures household consumption expenditures; investment ( $i_t$ ) is the sum of gross capital formation and inventory adjustments; net exports ( $nx_t$ ) is the difference between exports and imports of goods and services. Output,  $y_t$ , is the sum of  $c_t$ ,  $i_t$  and  $nx_t$ . We convert these data into real per capita values by using the CPI (1995 prices) from the IFS and population data drawn from the IFS. Civilian employment data and labor hours series, which correspond to weekly average hours worked in nonagricultural activities, are drawn from the OECD. Total hours worked,  $n_t$ , is defined as the product of hours worked per week and the employment rate normalized by the weekly time endowment, 168. The data is not subject to any filtering before it is fed into the model.

---

<sup>8</sup> We consider the small open economy setup since it provides a reasonable compromise between the closed economy and the two-country model. We do not study a two-country model since the predictions of the standard two-country models (Backus, Kehoe, and Kydland, 1995; and Kose and Yi, 2001) regarding the volatility and comovement features of output and consumption fluctuations are quite different than those observed in the data. Moreover, it is more complicated to establish a mapping between the observables and unobservables in a two-country setting.

<sup>9</sup> For Germany, our series end with the introduction of the euro.

#### IV. PARAMETER CALIBRATION

We use the equations (5)-(7) and data on market variables (output, consumption, and hours) to generate the series on unobserved nonmarket variables, which are home hours, home consumption, and leisure. To do this, we need first to calibrate  $\alpha_m, \alpha_n, \gamma_m, \gamma_l$  and  $\rho$ . Our benchmark experiment is run with the same parameterization of the model for all the countries. To help in comparing our results with those in IKS, we use their parameterization as a benchmark. We also consider alternative parameter combinations and study the country specific differences in our sensitivity experiments.

Following IKS, the parameter  $\alpha_m$  is set to 0.28 implying the share of labor income in the market sector is 0.72. These values are close to those used in several other studies in the literature. For example, using the postwar U.S. national income data, GRW (1993) estimate that  $\alpha_m$  is 0.29 in a model with household production and government expenditure. In an international business cycle model with home production, Canova and Ubide (1998) assume that  $\alpha_m$  is 0.36, a widely used value in the closed economy real business cycle literature.<sup>10</sup> In our sensitivity analysis section, we consider alternative values of  $\alpha_m$ .

As in most other studies focusing on the dynamics of business cycles of home production, including BRW and IKS, we assume that labor input plays a more important role in the home sector than in the market sector. In particular, we set  $\alpha_n$  to 0.14, which is equal to the value used by IKS. IKS argue that their choice is a reasonable one since it is equal to half of that they use for the capital share in the market sector. In standard calibration exercises involving models with home production, the capital share in the home sector is set to match the steady-state ratio of home output to market output and ranges from 0.08 in BRW to 0.32 in GRW. This implies that the share of labor income in the home sector is 0.86. We study how the business cycle properties change in response to the changes in this parameter in the sensitivity analysis section.

Following IKS, we assume that  $\gamma_m$  is equal to 0.4. This is consistent with other estimates in the literature. For example, using the hours series for the United States, BRW and Canova and Ubide (1998) estimate that  $\gamma_m$  is around 0.35. While  $\gamma_m$  affects the level of home consumption relative to market consumption, it does not have any implications for most of the moments we are interested in.

---

<sup>10</sup> Canova and Ubide (1998) borrow this value from Zimmerman (1995), who estimates the capital share of output using the data of several developed countries and reports that the average value of this parameter is around 0.36. Baxter and Jermann (1999) assume that the share of capital is 0.31 in the market sector in their model with home production.

It is straightforward to show that  $\gamma_l > .5$  is sufficient for  $l_t > h_m$ . Since sleep is included as leisure, this is a reasonable lower bound on our choice of  $\gamma_l$ . Following IKS, we assume that  $\gamma_l$  is equal to 0.73. Panel data on time use suggests that the mean of home hours is about 85% of the mean of market hours as discussed in the introduction. In our data this holds with  $\gamma_l$  equal to 0.71.

In several studies focusing on home production, the elasticity of substitution between home and market consumption goods is assumed to be positive. For example, Gronau (1986) and Eichenbaum and Hansen (1990) provide estimation results suggesting that the two goods are perfect substitutes, i.e., the value of  $\rho$  is equal to 1. BRW employ pooled data from the Panel Study of Income Dynamics (PSID) and estimate that  $\rho$  is equal to 0.6. Using maximum likelihood estimation, McGrattan, Rogerson, and Wright (1997) find that  $\rho$  is equal to 0.385 (with a standard error of 0.145). Rogerson, Rupert, and Wright (1995) employ PSID data and report that the estimates of  $\rho$  range from -0.065 for single males to 0.355 for married people.

IKS discuss the implications of alternative values of  $\rho$  and take an agnostic view about its value. In particular, IKS study two particular cases: when market and home consumption goods are complements and when the two are substitutes. In their benchmark experiment, the value of  $\rho$  is assumed to be 0.5 (the case of substitutes). We employ the same value in our benchmark experiments. However, an implication of this parameterization is that home productivity has fallen sharply since 1980 in the United States and Canada. Since it is hard to identify any evidence of this decline, we also consider the case where  $\rho$  is -1.5 (the case of complements). In this case, home productivity grows in both countries.

## V. RESULTS

### A. Time Series Behavior

While our focus in this paper is on the business cycle properties, we begin our discussion by observing the trend behavior of the key market series and each home series implied by our benchmark parameterization. In each panel of Figure 1, the dashed line shows the behavior of market hours, the lighter solid line shows leisure, and the darker solid line shows home hours for the benchmark parameterization.<sup>11</sup> In the United States and Canada, home hours have declined with the most notable decrease occurring since 1983. This decline did not occur in Japan and Germany. The different behavior of home hours across these countries in part reflects the behavior of market hours. While market hours increased from 1970 levels in the United States and Canada, they have decreased in Germany and Japan. In the United States, the fall in home hours has been larger than the increase in market hours. As a consequence, leisure has also risen slightly.

---

<sup>11</sup> We thank the Foundation for International Business Cycle Research (FIBER) for providing business cycle peak and trough dates.

Figure 1 also shows that leisure rises in each recession recorded in each of the countries. Since market hours are well known to be procyclical, this suggests that in recessions leisure in part replaces market hours. However, changes in leisure tend to be smaller than those in market hours during recessions. This requires that home hours also rise during recessions. Though the cyclical behavior of home hours tends to be less pronounced as we discuss later, home hours are higher during some recession episodes. Thus, it appears that time out of employment during recessions increases both leisure and home hours.

In each panel of Figure 2, the dashed lines show the behavior of market output, the lighter solid line shows market consumption, and the darker solid line shows home consumption for the benchmark parameterization. In the United States and Canada, the decrease in home hours has resulted in a slight decrease in home output. In Japan and Germany, home output has increased. Figure 2 also suggests home consumption is acyclical or weakly procyclical in the each country. During the 1969-70, 1980, and 2001 recessions, home output increased in the United States. In the 1973-75 and 1990-91 recessions, home consumption fell early in the recession and rose prior to the recession's end. In the 1980-81 recession, home output fell. In Canada, home hours rose in one recession and were largely unchanged in the other over this period. In the remaining countries, there is again no clear relationship between market and home sector output.

While the behavior of our home hours and leisure series are independent of  $\rho$  (see equations (5) and (6)), the behavior of home consumption depends critically on  $\rho$ . Figure 3 demonstrates this dependence for the United States and Canada. Each panel shows home consumption at two values of  $\rho$ . The darker line is the same series as in Figure 2; i.e.  $\rho=0.5$ . The lighter solid line is home consumption with  $\rho=-1.5$ . When market and home consumption are relative complements ( $\rho=-1.5$ ), the behavior of the home series is much different for the United States and Canada. In this case, increased market output implies increased production of complementary home output as well.

## **B. Stylized Features of Business Cycle Dynamics**

We now focus more carefully on the business cycles properties of the major market and home sectors variables in each country. In particular, we study the following features of business cycle fluctuations: volatility as measured by the percentage standard deviation, persistence as measured by the first-order autocorrelation coefficient, and the degree of contemporaneous correlation as measured by the correlation coefficients. Before calculating the moments, we logged and HP filtered all data series. We also provide a detailed comparison of our results with those in the earlier literature that studies the dynamics of the home sector.

### ***Volatility***

Table 1 displays the volatility of the major market and home variables relative to that of output. Recall that market variables are the observed data series. Our findings regarding these are similar to findings in a number of other studies and the results are similar across countries. Consumption is less volatile than output, and investment is on average roughly

three times more volatile than output. The relative volatility of net exports is between the relative volatility of investment and output in all countries except Japan where net exports is the most volatile variable. Market hours are also less volatile than output, and its relative standard deviation is on average close to that of consumption.

Our home series (including leisure) are derived from applying the observables to the mapping implied by the model. Thus, they depend on the observed data, our model, and our choice of parameters. For our benchmark parameters, several interesting regularities emerge. Notice first that the volatility of home hours is slightly larger than that of market hours in each country, while leisure is the least volatile series. The standard deviation of leisure is roughly 9 percent as large as that of output. The relative volatility of home hours is around 80 percent.

The low variability in leisure is partly explained by equation (5). Given our parameterization  $\frac{1-\alpha_n}{1-\alpha_m} \approx 1.19$ . The average value of  $\frac{c_{mt}}{y_{mt}}$  is 0.82 in the United States and is similar in other the other countries. Given this  $\left(1 - \frac{c_{mt}}{y_{mt}} \frac{1-\alpha_n}{1-\alpha_m}\right)$  is close to 0 so that changes in  $h_{mt}$  will not result in large changes in leisure. Changes in  $\frac{c_{mt}}{y_{mt}}$  will not have a large effect on leisure for the same reason. Also these changes are scaled by  $h_{mt}$ , which is 0.14 on average, which further diminishes its impact. If we maintain our assumption that market production is more capital-intensive than home production,  $\alpha_n$  is constrained to lie  $[0, 0.28]$ . Over this range, the low standard deviation of leisure is very robust, ranging from 0.0652 to 0.0663 for the United States.

From (6) it is clear that a change in market hours will have a relatively larger impact on home hours giving rise to its greater volatility on average  $\left(1 + \frac{c_{mt}}{y_{mt}} \frac{\gamma_l}{1-\gamma_l} \frac{1}{1-\alpha_m}\right)$  is clearly not close to 0). In each country, the volatility of home hours is close to that of market hours. Home output, which is equal to home sector output in the model, is more volatile than market output. In particular, the volatility of home output relative to market output ranges from 1.9 in the United States to 3.6 in Germany.

The final rows of Table 1 report volatility in labor productivity  $\left(\frac{y_{mt}}{h_{mt}}, \frac{y_{ht}}{h_{ht}}\right)$  and the Solow residuals. Solow residual series are calculated employing the production functions of the two sectors.<sup>12</sup> To be more specific, the Solow residuals in logarithms are calculated using the following formulas:

---

<sup>12</sup> Following Backus, Kehoe, and Kydland (1995), we ignore the capital stock series since comprehensive data on quarterly capital stock is not available.

$$\log(A_{mt}) = \log(y_{mt}) - (1 - \alpha_m) \log(h_{mt})$$
$$\log(A_{nt}) = \log(y_{nt}) - (1 - \alpha_n) \log(h_{nt}).$$

In each country, the volatility of home Solow residuals is greater than the volatility of market Solow residuals and greater than the volatility of output, ranging from 1.3 to 2.61.

Our results pertaining to the U.S. data series are consistent with the qualitative finding of IKS (1997). For example, they find that home consumption is more volatile than market consumption, that market hours fluctuate about as much as home hours, and that leisure is the least volatile series. Moreover, we show that each of these findings holds across all counties in our data suggesting robustness. Quantitatively, our results differ modestly from IKS. They find that the relative standard deviations of market hours and home hours are 0.77 and 0.61, compared to 0.61 and 0.67 in our study. Considering that our market hours series comes from a different source and covers a different time period, moderate differences are unsurprising.

IKS also find the relative standard deviations of market and home consumption to be 0.43 and 1.01 compared to 0.71 and 1.90 in our study. This disparity arises in part because our consumption series includes both durable and nondurable consumption components, whereas their series includes only nondurable consumption series. Durable consumption goods are known to be two to three times more volatile than nondurable consumption series (see Baxter, 1996). Its inclusion then increases the volatility of both market and home consumption series.

As mentioned above, studies by BRW, Gomme, Rupert, and Kydland (GKR, 2001), and Baxter and Jermann (1999) employ closed economy business cycle models with a home production sector and calibrate their models to represent the U.S. economy. They make simplifying assumptions about the process of home productivity shocks, feed these shocks to the model to obtain simulated data series, and report the moments of these series. Typically, business cycle researchers compare the moments of their generated series with those of observed data to judge whether the model is successful in replicating observed business cycles. In the case of the home sector, such comparisons are made impossible by data limitations. However, by comparing our moments with theirs we are able at least to gauge the extent to which their models replicate the business cycle properties of the data series implied by our model.

As in our data, GKR find that home consumption is more volatile than market consumption. The results by BRW and Baxter and Jermann (1999) also suggest that home hours are about as volatile as market hours. In a related study, Canova and Ubide (1997) simulate a two-country business cycle model augmented with a home production sector. They find that when the model is subjected to only home productivity shocks, the relative volatility of home and market hours are 1.30 and 0.98. When the model is simulated with both market and nonmarket productivity shocks, the relative volatility of home hours is very close to that of market hours. Our results are broadly consistent with these findings.

### *Persistence*

Table 2 presents persistence of the series under investigation. The autocorrelation of output is on average 0.82 and it ranges from 0.78 in Germany to 0.88 in the United States. Market consumption, market hours, investment, and the net exports series are quite persistent as well. Home sector variables seem to be less persistent than the market variables. For example, the autocorrelation of home consumption is significantly less than that of market consumption in all countries. Similarly, hours employed in the home sector exhibit less inertia than those in the market sector in all countries. However, leisure is highly persistent, with an average autocorrelation coefficient of 0.74.

### *Comovement*

Table 3 documents the contemporaneous correlations of the major market and nonmarket variables with output. As one would expect, consumption, market hours, and investment are procyclical and the net exports series are countercyclical in all countries. Average labor productivity in the market sector is highly correlated with output (0.75) and the fluctuations in the Solow residuals of the market sector closely follow those in sectoral output (near 1).

There is little correlation between home consumption (output) and market output. This correlation ranges from a low of -0.14 in the United States to a high of 0.12 in Germany. Home hours series are on average negatively correlated with market output ranging from -.11 in Germany to -.47 in the United States. The correlation coefficient between leisure and market output does not change much across countries, as leisure is highly countercyclical in all countries with an average correlation of -0.79 with output. Equation (5) suggests that there is a positive correlation between leisure and the ratio of market consumption to output. The ratio of market consumption to output is countercyclical in the data. Thus, leisure is negatively correlated with market output.

We also study lead and lag correlations, which are not presented in a table for space considerations. Leisure and home hours are both countercyclical at all leads and lags. The (absolute value of the) correlation between leisure and output is larger than that between home hours and output at all leads and lags in all countries. Also in each country, both home hours and leisure are negatively correlated with market hours. Typically, this correlation is larger (in absolute value) for home consumption. The average contemporaneous correlation between home and market hours is -0.67, and the average contemporaneous correlation between leisure and market hours is -0.79. From these, we conclude that a decrease in market hours is offset by increases in both leisure and home hours. However, as discussed previously, the volatility of leisure is quite small in comparison to the volatility of market hours and home hours. Thus in large part, an increase in market hours results in decreased home hours (and vice versa) as displayed in Figure 1.

The correlation between home hours and leisure is small but differs across countries; it is positive in all countries studied but Canada. The correlation between market consumption and home consumption is negative in all countries (except Germany) and ranges from -0.33 in Canada to only 0.03 in Germany. This implies that increases in market consumption at



times coincide with decreases in home consumption and vice versa. While there is a large positive correlation between home sector output (consumption) and home hours, the correlation between home output and leisure series is negative in all countries except Germany.

Our findings also confirm the qualitative findings of previous simulation studies. For example, IKS find home hours and leisure series are countercyclical in the United States. We also find that home hours are negatively correlated with market output (-0.47) and our leisure series are also negatively correlated with market output (-0.77) in the United States. BRW, GKR, and Canova and Ubide find that home hours are highly countercyclical. Baxter and Jermann find home sector output is positively correlated with market output. However, in each paper the correlation is not always large, ranging from 0.1 to 0.3 and from 0.11 to 0.36. In our findings this ranges from -0.14 in the United States to 0.12 in Germany. Thus while some quantitative differences exist between our results and theirs, this is to be expected given the differences between our approaches and data sets. The finding that the two outputs are not highly correlated largely holds.

### ***Driving processes***

A problem facing researchers who work with dynamic business cycle models including a home sector is that they do not have the requisite data to estimate productivity disturbances for this sector. Hence, they use simplifying assumptions regarding the home productivity shock processes. Our approach allows us to evaluate whether these assumptions are reasonable. We assume that productivity disturbances follow a Markov process

$$A_{t+1} = \pi A_t + \varepsilon_{t+1}$$

where  $A_t = [\ln(A_{mt}) \ \ln(A_{ht})]'$  and  $\varepsilon_t \sim N(0, \Sigma)$ . This specification, which is widely used in the literature, allows us to examine the role of intersectoral spillovers.<sup>13</sup>

Table 4 documents our findings. There are four major results. First, both market and home productivity shocks are highly persistent. Second, the sectoral feedback coefficient is small in absolute value in all cases. This suggests it is safe to assume that technological spillovers between market and home sectors are mostly negligible. Third, the standard deviation of the home productivity disturbance is roughly three times larger than that of the market disturbance. Fourth, the contemporaneous correlation between market and home productivity shocks is large and positive in all countries.

---

<sup>13</sup> Our major findings are robust to several alternative specifications which take into account the role of intersectoral and intercountry productivity spillovers. The results of these additional estimations are available from the authors upon request.

BRW assume that both the market and home productivity shocks follow the same process for the United States. GRW and Baxter and Jermann employ the same shock processes as those used by BRW. In particular, the persistence coefficient of each shock is equal to 0.95 and the standard deviation of each disturbance is 0.007. They assume that the correlation between the market and home disturbances is 0.67. Our estimations provide empirical evidence supporting some of these assumptions. We find that the persistence coefficient is around 0.94, which is almost identical to the figure BRW used, for both sectors. The standard deviation of the market disturbance is (0.011) in our study, which is only slightly larger than that of BRW (0.007). However, we also find that the volatility of the home disturbance is roughly three times larger than that of the market disturbance. This conflicts with their assumption of equal volatility of disturbances. The correlation between the two disturbance terms is 0.33 in our study. This is roughly half of the number BRW used. These findings suggest that previous studies consistently underestimate the volatility of home sector productivity shocks while overestimating the correlation between home and market sector productivity disturbances.

Canova and Ubide (1997) assume that the persistence parameter is 0.84 and the standard deviation is 0.007 for both sectors in their open economy business cycle model. They take the correlation between the sectoral disturbances from the BRW study. The intersectoral spillover term is equal to 0.088 in their study. Our estimations indicate that it is reasonable to ignore the sectoral spillover term.

### *Cross-country correlations*

There has been a large and growing body of research that studies the international dynamics of business cycles using stochastic dynamic business cycle models.<sup>14</sup> An important objective of this research program is to assess the cross-country similarities and differences in business cycle fluctuations. While this research program has paid considerable attention to the comovements in market variables, cross-country dynamics of home sector variables have not been studied due to the data limitations. Since we produce comparable data on unobservable home sector aggregates, we document the similarity of business cycle behavior across countries by studying the contemporaneous cross-country correlations of the major market and home sector variables.

Table 5 presents our findings. In most cases, cross-country output correlations are larger than those of consumption correlations. Stochastic dynamic business cycle models are not able to generate this empirical regularity, and this gap between the theory and data is called “the quantity anomaly” by Backus, Kehoe, and Kydland (1995). Investment correlations are

---

<sup>14</sup> Christodoulakis, Dimelis, and Kollintzas (1995) find that there are important similarities in the time series properties of labor hours across industrialized economies. Backus, Kehoe, and Kydland (1995) find that the volatility of employment varies from 0.34 to 1.23 in a sample of major industrialized countries. They explain this large disparity with international differences in labor market experience. Kose, Otrok, and Whiteman (2003) provide a brief survey of the literature, which focuses on the similarities of business cycles across countries.

positive and smaller than those of output in most cases. Fluctuations in market hours tend to be positively correlated across countries, suggesting that the cyclical dynamics in the market sector might have some common features despite the fact there exist major differences in the structural characteristics of labor markets across countries. Net exports have no common pattern, but most of correlations are negative. Cross-country correlations of the fluctuations in the market Solow residuals are positive in all cases. Correlations of market productivity are often positive, but they are relatively low, and in most cases lower than those of output.

Overall, home sector variable correlations tend to be lower than their market sector counterparts. Since home output is not a tradable good, this is to be expected. We find that correlations of home consumption (output) are smaller than those of both market output and market consumption. Not surprisingly, correlations of home consumption do not exhibit a clear pattern: four of the six correlations are low and negative while others are low and positive. Cross-country correlations of home hours are smaller than those of market hours in all countries. Leisure series exhibit much higher correlation across countries than home hours do, with all correlation pairs positive. Home productivity correlations do not display much regularity, but most correlations are negative. These correlations are lower than those of market productivity in all cases. Correlations of the Solow residuals of the home sector are low, and they are lower than those of the market sector.

### C. Sensitivity Analysis

We conduct an extensive sensitivity analysis, which is available upon request. Our principle findings prove to be quite robust. Here we highlight a few items from this analysis. We argue above that the business cycle properties of leisure will depend only on  $\frac{1-\alpha_n}{1-\alpha_m}$ , while home hours will depend upon  $\frac{\gamma_l}{1-\gamma_l} \frac{1}{1-\alpha_m}$  and home consumption on both  $\frac{1}{1-\alpha_m} \frac{\gamma_l}{1-\gamma_l}$  and  $\rho$ .

For ease of comparison, we have conducted all of our analysis up to this point with the same parameterization for each country. An alternative approach would be to calibrate each country differently. Zimmermann (1995) reports estimates of  $\alpha_m$  for each of the countries in our analysis ranging from 0.37 for the United States to 0.42 for Canada.<sup>15</sup> We find only minor quantitative changes in the results when we use the country specific values. We also experiment with  $\alpha_m = 0.36$  since this is a widely used value in the literature. When the capital share increases to 0.36 from 0.28 in the market sector, this leads to small increases in the relative volatilities of home consumption (output), home hours, and home productivity and generates only minor changes in the correlations of these variables with market output. For example, the volatility of home consumption (hours) goes up to 2.27 (0.86) percent from 1.9 (0.67) percent when  $\alpha_m$  rises to 0.36 from 0.28. Our findings regarding the leisure series are also qualitatively robust to alternative choices of  $\alpha_n$  over the relative range.

---

<sup>15</sup> His estimates range from 0.42 for Canada to 0.37 for the United States.

The preference parameter  $\gamma_i$  has a modest effect on both home hours and home consumption. In each country home output becomes less volatile as we decrease this value. With  $\gamma_i = 0.5$  home consumption is 1.57 times as volatile as market output on average. Hours in home production become less volatile in each country. The correlation of home output with market output increases and the correlation of home production hours with market output becomes more negative in each country. However, cross-country correlations do not change in a consistent way. As we discuss earlier in the paper, changes in  $\gamma_m$  do not affect the business cycle moments, but lead to shifts in the level of imputed home consumption series.

In each country, home output becomes less volatile when we decrease  $\rho$  to -1.5 but it remains more volatile than market output. On average home output is 2.58 times as volatile as market output with  $\rho = 0.5$  and only 1.34 times as volatile with  $\rho = -1.5$ . This is an intuitively appealing result as it shows that when the two goods are complements, substitution across them diminishes and the volatility of home output goes down. Persistence of home output also increases slightly on average. Not surprisingly, the comovements of home sector output with market output and market consumption depend on the extent to which these goods are substitutes. With  $\rho = 0.5$ , the average correlations of home output with market output and market consumption are 0.05 and -0.17. With  $\rho = -1.5$  these are 0.54 and 0.77.

## VI. CONCLUSION

Recent empirical studies find that the value of household production activities is as much as 50 percent of aggregate output in several developed countries. Moreover, recent research suggests that studying the dynamics of business cycles in home production is an important component of the modern business cycles research program. However, comparable time series data on home production activities are not available, since these activities are not observable. Our paper attempts to provide a comprehensive cross-country study of the stylized features of cyclical fluctuations in home production activities using an approach that is complementary to the standard approach.

The results suggest that there are important similarities in the business cycle properties of the home sector across countries. First, we find that home production is more volatile than market production, that market and home sector hours have similar volatility, and that leisure is much less volatile than other uses of time in all countries. Second, leisure is highly countercyclical in all countries and home hours are countercyclical in all countries. Third, home production variables exhibit less persistence than market variables. Fourth, we find that home production is not highly correlated with market output. Cross-country correlations related to home production tend to be lower than those of market production for both consumption and hours series.

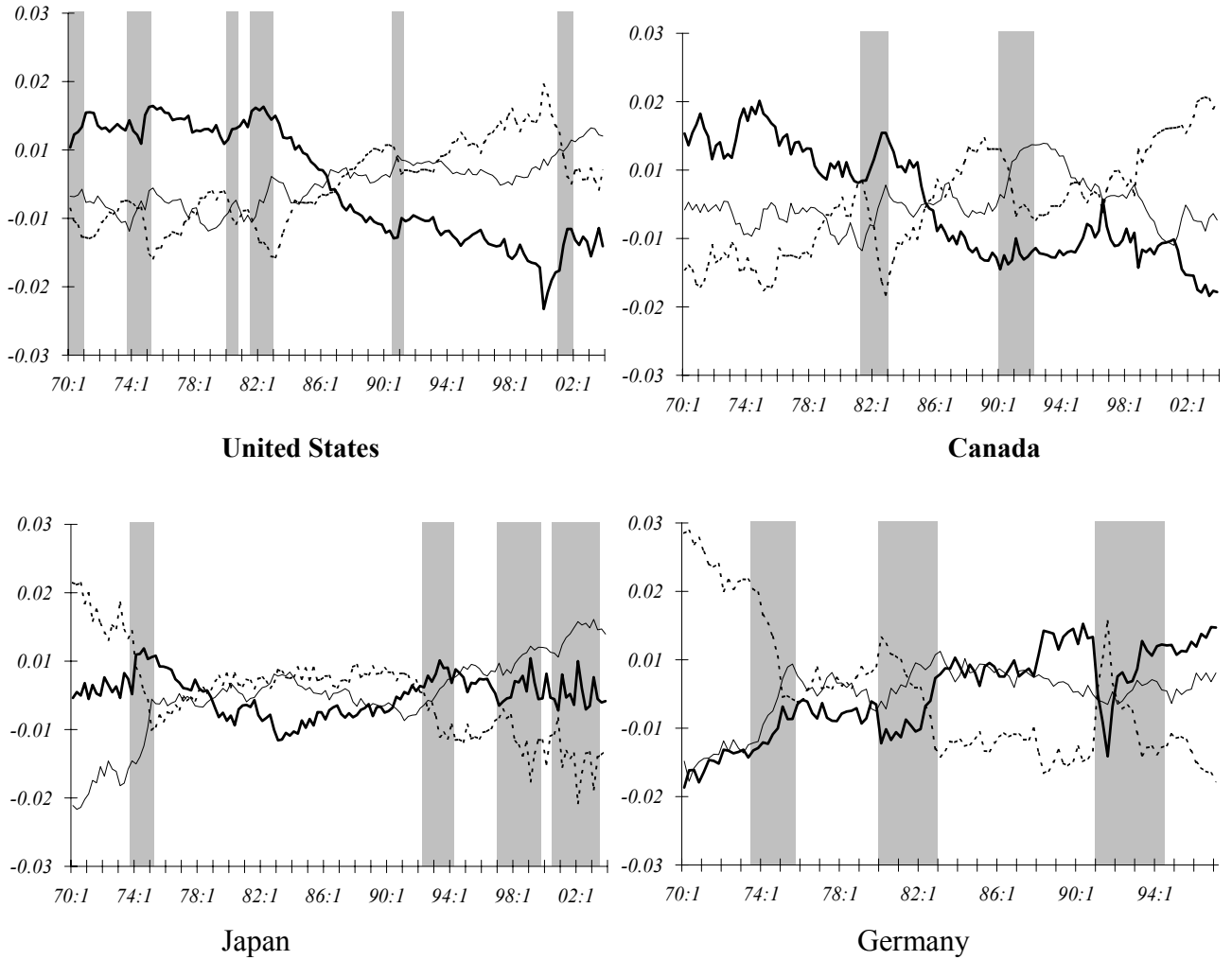
There are some dimensions along which our results differ from previous studies. For example, our findings suggest that previous studies consistently underestimate the volatility of home sector productivity shocks while overestimating the correlation between home and market sector productivity disturbances. While there are some other minor differences

between the features of the home sector business cycles we found and those reported in the previous studies, there are also striking similarities. Because we employ a complementary approach, we take this as evidence of the appropriateness of their assumptions and the robustness of some of their results.

The IKS approach that we employ has similarities with the standard business cycle approach. Both require calibrated dynamic, stochastic business cycle models to generate time series for the home sector. In each case, these series are specific to the model and to the choice of parameters. Reservations regarding the choice of parameters can easily be addressed through sensitivity analysis. We conduct such an analysis and find our results to be robust. Reservations regarding the choice of model are not so easily addressed. When one uses “theory for measurement,” the theory used is important. For this reason, we stay close to familiar ground. Our model differs from IKS in a very modest way. IKS, in turn, builds on a frequently employed theoretical framework. Given this, and given that our results are consistent with the standard approach and consistent across countries, we argue that our exercise provides important and robust insights into the cyclical behavior of home production.

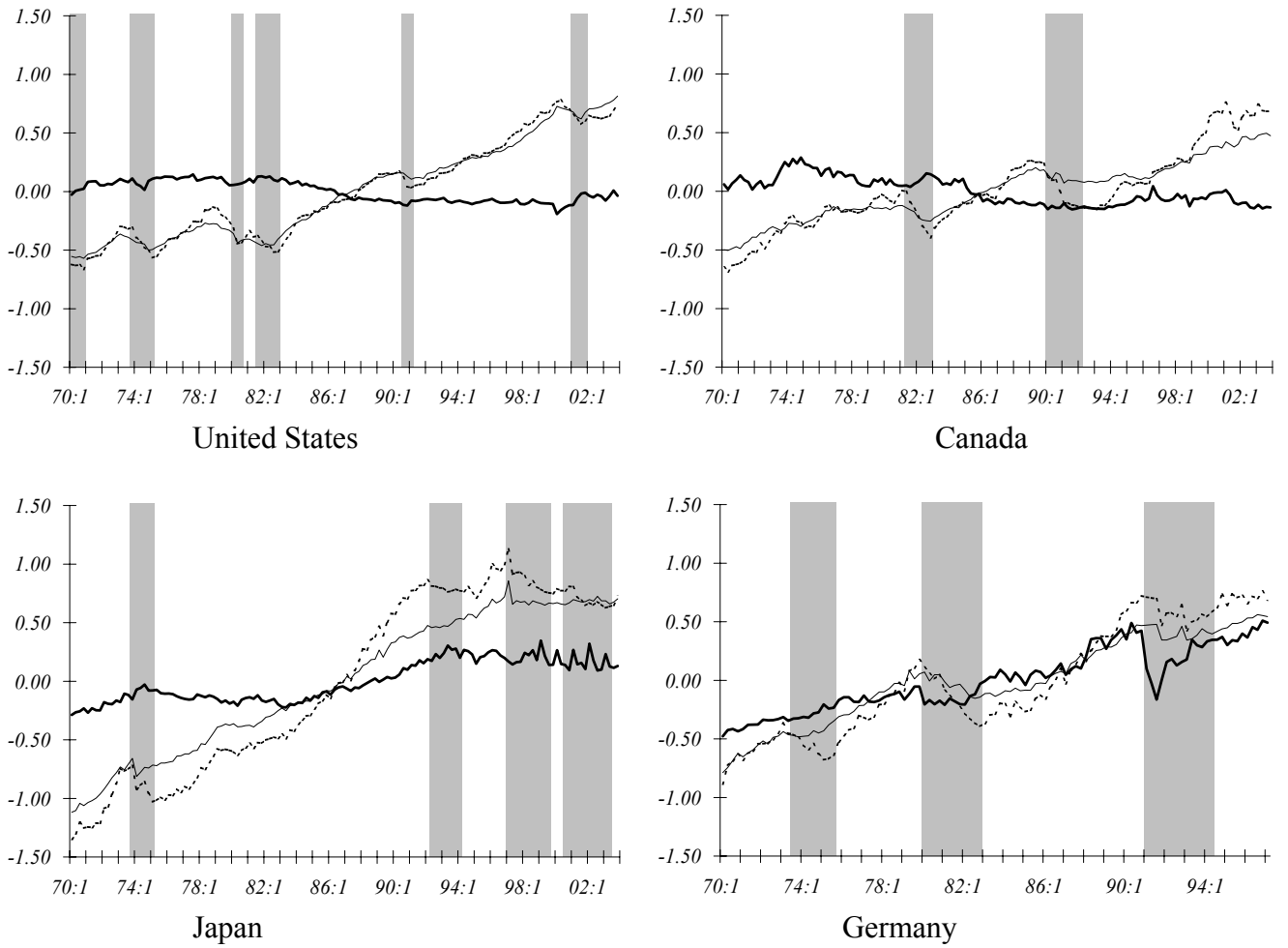
There are some interesting questions which can be explored in future research. For example, we do not study the roles of fiscal and monetary policies, which can affect the dynamic interactions between home and market sectors in our model. Moreover, understanding the dynamics of household production is a very useful exercise for developing countries where home production activities account for a much larger fraction of aggregate output.

**Figure 1**  
**Hours**



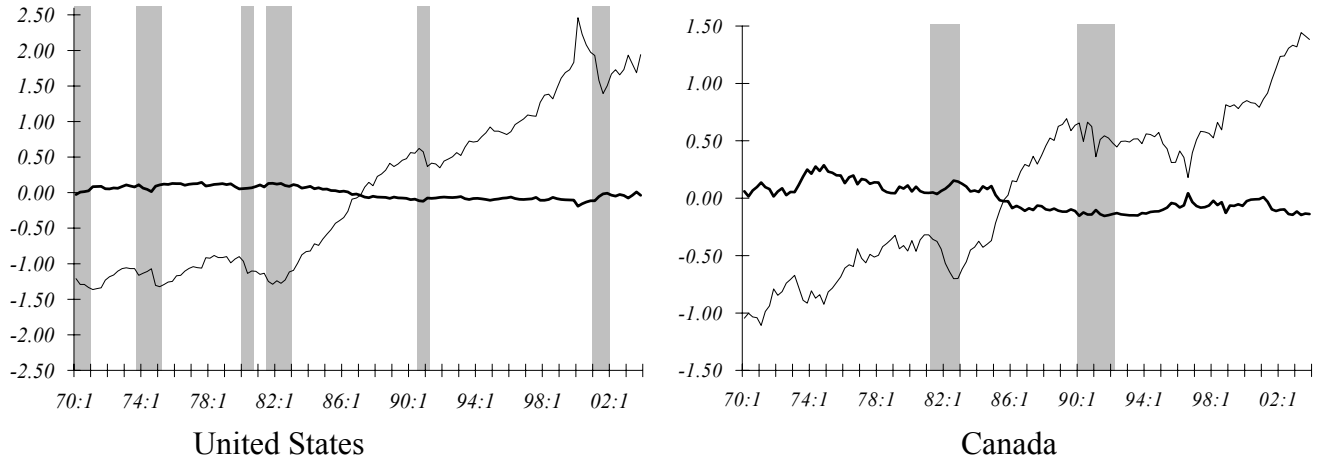
*Notes: Market hours (dashed line), leisure (lighter solid line), and home hours (darker solid line). The mean value is subtracted from each series. Shaded regions represent periods of recession.*

**Figure 2**  
**Output and Consumption**



*Notes: Market output (dashed line), market consumption (lighter solid line), and home consumption under the benchmark parameterization (darker line). The mean value is subtracted from each series. Shaded regions represent periods of recession.*

**Figure 3**  
**Home Consumption**



*Notes: Home consumption at the benchmark parameterization and  $\rho = 0.5$  (darker solid line) and home consumption with  $\rho = -1.5$  (lighter solid line). The mean value is subtracted from each series. Shaded regions represent periods of recession.*



**Table 1**  
**Relative Volatility**

	<b>United States</b>	<b>Canada</b>	<b>Germany</b>	<b>Japan</b>	<b>Mean</b>	<b>Std. Dev.</b>
<b>Market Output</b>	1	1	1	1	1	0
<b>Market Consumption</b>	0.71	0.56	0.66	0.77	0.68	0.09
<b>Market Hours</b>	0.61	0.68	0.87	0.62	0.70	0.12
<b>Investment</b>	3.22	2.78	2.42	2.38	2.70	0.39
<b>Net Exports</b>	2.14	1.26	1.66	4.08	2.29	1.25
<b>Home consumption (output)</b>	1.9	2.42	3.59	2.39	2.58	0.72
<b>Home hours</b>	0.67	0.71	1.02	0.72	0.78	0.16
<b>Leisure</b>	0.06	0.1	0.09	0.09	0.09	0.02
<b>Market Labor Productivity</b>	0.62	0.63	0.99	0.78	0.76	0.17
<b>Market Solow Residual</b>	0.87	0.86	0.92	0.9	0.89	0.03
<b>Home Labor Productivity</b>	1.3	1.75	2.61	1.73	1.85	0.55
<b>Home Solow Residual</b>	1.81	2.32	3.45	2.29	2.47	0.70

*Notes: All variables, except net exports, are logged and then HP filtered. Net exports is normalized by output, then HP filtered. See text for details.*

**Table 2**  
**Persistence**

	<b>United States</b>	<b>Canada</b>	<b>Germany</b>	<b>Japan</b>	<b>Mean</b>	<b>Std. Dev.</b>
<b>Market Output</b>	0.88	0.85	0.78	0.78	0.82	0.05
<b>Market Consumption</b>	0.89	0.76	0.73	0.62	0.75	0.11
<b>Market Hours</b>	0.83	0.8	0.79	0.48	0.73	0.16
<b>Investment</b>	0.83	0.8	0.73	0.88	0.81	0.06
<b>Net Exports</b>	0.81	0.64	0.68	0.88	0.75	0.11
<b>Home consumption</b>	0.57	0.59	0.68	0.26	0.53	0.18
<b>Home hours</b>	0.67	0.64	0.68	0.31	0.58	0.18
<b>Leisure</b>	0.72	0.8	0.67	0.75	0.74	0.05
<b>Market Labor Productivity</b>	0.79	0.6	0.72	0.48	0.65	0.14
<b>Market Solow Residual</b>	0.88	0.81	0.76	0.75	0.80	0.06
<b>Home Labor Productivity</b>	0.55	0.58	0.68	0.26	0.52	0.18
<b>Home Solow Residual</b>	0.57	0.59	0.68	0.26	0.53	0.18

*Notes: All variables, except net exports, are logged and then HP filtered. Net exports is normalized by output, then HP filtered. See text for details.*

**Table 3**  
**Comovement**

	<b>United States</b>	<b>Canada</b>	<b>Germany</b>	<b>Japan</b>	<b>Mean</b>	<b>Std. Dev.</b>
	<i>c(x(t),y(t))</i>	<i>c(x(t),y(t))</i>	<i>c(x(t),y(t))</i>	<i>c(x(t),y(t))</i>		
<i>x</i>			<u><i>y=Market</i></u>			
			<u><i>output</i></u>			
<b>Market Output</b>	1	1	1	1	1.00	0.00
<b>Market Consumption</b>	0.91	0.78	0.86	0.84	0.85	0.05
<b>Market Hours</b>	0.81	0.78	0.45	0.62	0.67	0.17
<b>Investment</b>	0.93	0.83	0.91	0.84	0.88	0.05
<b>Net Exports</b>	-0.47	0.03	-0.18	-0.32	-0.24	0.21
<b>Home consumption</b>	-0.14	0.1	0.12	0.11	0.05	0.13
<b>Home hours</b>	-0.47	-0.19	-0.11	-0.24	-0.25	0.15
<b>Leisure</b>	-0.77	-0.89	-0.79	-0.72	-0.79	0.07
<b>Market Labor Productivity</b>	0.82	0.75	0.62	0.79	0.75	0.09
<b>Market Solow Residual</b>	0.99	0.99	0.97	0.99	0.99	0.01
<b>Home Labor Productivity</b>	0.04	0.21	0.21	0.24	0.18	0.09
<b>Home Solow Residual</b>	-0.12	0.11	0.13	0.12	0.06	0.12
<i>x</i>			<u><i>y= Market</i></u>			
			<u><i>Hours</i></u>			
<b>Home hours</b>	-0.8	-0.7	-0.89	-0.78	-0.79	0.08
<b>Leisure</b>	-0.7	-0.66	-0.62	-0.68	-0.67	0.03
<i>x</i>			<u><i>y= Home</i></u>			
			<u><i>hours</i></u>			
<b>Leisure</b>	0.14	-0.07	0.2	0.06	0.08	0.12
<i>x</i>			<u><i>y= Home</i></u>			
			<u><i>consumption</i></u>			
<b>Market consumption</b>	-0.26	-0.33	0.03	-0.11	-0.17	0.16
<b>Home hours</b>	0.93	0.96	0.97	0.94	0.95	0.02
<b>Leisure</b>	-0.1	-0.31	0.04	-0.14	-0.13	0.14
<i>x</i>			<u><i>y= Market</i></u>			
			<u><i>Solow Residuals</i></u>			
<b>Home Solow Residual</b>	-0.02	0.24	0.35	0.25	0.21	0.16

*Notes: All variables, except net exports, are logged and then HP filtered. Net exports is normalized by output, then HP filtered. See text for details.*

**Table 4**  
**Driving Processes**

	<b>Persistence of Shocks</b> $\pi$	<b>Variance-Covariance Matrix</b> $\Sigma$
<b>United States</b>	$\begin{bmatrix} 0.94 & -0.01 \\ (0.03) & (0.01) \\ -0.13 & 0.91 \\ (0.10) & (0.03) \end{bmatrix}$	$\begin{bmatrix} 0.011^2 & 0.33 \\ & 0.040^2 \end{bmatrix}$
<b>Canada</b>	$\begin{bmatrix} 0.95 & 0.00 \\ (0.03) & (0.01) \\ 0.01 & 0.92 \\ (0.11) & (0.04) \end{bmatrix}$	$\begin{bmatrix} 0.013^2 & 0.54 \\ & 0.052^2 \end{bmatrix}$
<b>Germany</b>	$\begin{bmatrix} 0.93 & 0.02 \\ (0.03) & (0.01) \\ 0.01 & 0.85 \\ (0.12) & (0.06) \end{bmatrix}$	$\begin{bmatrix} 0.016^2 & 0.54 \\ & 0.067^2 \end{bmatrix}$
<b>Japan</b>	$\begin{bmatrix} 1.03 & -0.03 \\ (0.02) & (0.01) \\ 0.35 & 0.79 \\ (0.10) & (0.05) \end{bmatrix}$	$\begin{bmatrix} 0.014^2 & 0.41 \\ & 0.058^2 \end{bmatrix}$
<b>Mean</b>	$\begin{bmatrix} 0.95 & 0.03 \\ (0.03) & (0.01) \\ 0.10 & 0.85 \\ (0.12) & (0.04) \end{bmatrix}$	$\begin{bmatrix} 0.014^2 & 0.34 \\ & 0.038^2 \end{bmatrix}$

*Notes:  $A_{t+1} = \pi A_t + \varepsilon_{t+1}$  where  $A_t = [\ln(A_{mt}) \ln(A_{nt})]'$  and  $\varepsilon_t \sim N(0, \Sigma)$ . Standard errors associated with the coefficients are reported in parenthesis. The off-diagonal term in the variance-covariance matrix represents the correlation between the innovations. See text for details.*

**Table 5**  
**Cross-Country Correlations**

<b>Table 5</b>							
<b>Cross-Country Correlations</b>							
<b>Output</b>					<b>Home Consumption</b>		
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	0.452				<b>Canada</b>	-0.172	
<b>Germany</b>	0.522	0.404			<b>Germany</b>	-0.148	0.017
<b>Japan</b>	0.482	0.157	0.496		<b>Japan</b>	-0.135	0.021
							-0.255
<b>Consumption</b>				<b>Home Hours</b>			
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	0.543	0	0	<b>Canada</b>	0.112		
<b>Germany</b>	0.394	0.419	0	<b>Germany</b>	-0.177	0.051	
<b>Japan</b>	0.338	0.025	0.346	<b>Japan</b>	-0.026	0.027	-0.138
<b>Market Hours</b>				<b>Leisure</b>			
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	0.619			<b>Canada</b>	0.433		
<b>Germany</b>	0.203	0.157		<b>Germany</b>	0.426	0.279	
<b>Japan</b>	0.335	0.211	0.413	<b>Japan</b>	0.476	0.217	0.438
<b>Market Productivity</b>				<b>Home Productivity</b>			
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	-0.152			<b>Canada</b>	-0.27		
<b>Germany</b>	0.369	0.18		<b>Germany</b>	-0.082	0.019	
<b>Japan</b>	0.179	0.033	0.053	<b>Japan</b>	-0.144	0.022	-0.26
<b>Market Solow Residuals</b>				<b>Home Solow Residuals</b>			
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	0.344			<b>Canada</b>	-0.183		
<b>Germany</b>	0.523	0.388		<b>Germany</b>	-0.143	0.017	
<b>Japan</b>	0.441	0.128	0.4	<b>Japan</b>	-0.137	0.021	-0.257
<b>Investment</b>				<b>Net Exports</b>			
	United States	Canada	Germany		United States	Canada	Germany
<b>Canada</b>	0.425			<b>Canada</b>	-0.107		
<b>Germany</b>	0.446	0.212		<b>Germany</b>	-0.062	0.132	
<b>Japan</b>	0.207	0.203	0.421	<b>Japan</b>	-0.494	-0.257	0.015

*Notes: All variables, except net exports, are logged and then HP filtered. Net exports is normalized by output, then HP filtered. See text for details.*

## References

- Backus, David K., Patrick J. Kehoe, and Finn E. Kydland, 1995, "International Business Cycles: Theory and Evidence," in *Frontiers of Business Cycle Research*, ed. by Thomas Cooley (Princeton, New Jersey: Princeton University Press), pp. 331-57.
- Baxter, Marianne, 1996, "Are Consumer Durables Important for Business Cycles?" *Review of Economics and Statistics*, Vol. LXXVIII, pp. 147-55.
- Baxter, Marianne, and Urban J. Jermann, 1999, "Household Production and the Excess Sensitivity of Consumption to Current Income," *American Economic Review*, Vol. 89, pp. 902-20.
- Baxter, Marianne, and Robert G. King, 1998, "Productive Externalities and Business Cycles," Working Paper (Charlottesville, Virginia: University of Virginia).
- Beauchemin, Kenneth R., 2000, "Whither the Stock of Public Capital?" Working Paper (Albany, New York: State University of New York at Albany).
- Benhabib, Jess, Richard Rogerson, and Randall Wright, 1991, "Homework on Labor Economics: Household Production and Aggregate Fluctuations," *Journal of Political Economy*, Vol. 99, pp. 1166-87.
- Bertola, Giuseppe, and Richard Rogerson, 1997, "Institutions and Labor Reallocation," *European Economic Review*, Vol. 41, pp. 1147-72.
- Blankenau, William M., Ayhan Kose, and Kei-Mu Yi, 2001, "Can World Real Interest Rates Explain Business Cycles in a Small Open Economy?" *Journal of Economic Dynamics and Control*, Vol. 25, pp. 867-99.
- Bonke, Jens, 1992, "Distribution of Economic Resources: Implications of Including Household Production," *Review of Income and Wealth*, Vol. 38, pp. 281-93.
- , 1995, "Education, Work and Gender: An International Comparison," Working Paper EUF 95/4 (Florence: European University Institute).
- Busato, Francesco, and Bruno Chiarini, 2004, "The Non-Market Sector in Europe and in the United States: Underground Activities and Home Production," Working Paper (Naples: University of Napoli).
- Canova, Fabio, and Angel J. Ubide, 1998, "International Business Cycles, Financial Markets and Household Production," *Journal of Economic Dynamics and Control*, Vol. 22, pp. 545-72.

- Christodoulakis, Nicos, Sophia P. Dimelis, and Tryphon Kollintzas, 1995, "Comparisons of Business Cycles in the EC: Idiosyncrasies and Regularities," *Economica*, Vol. 62, pp. 1-27.
- Eichenbaum, Martin, and Lars P. Hansen, 1990, Estimating Models with Intertemporal Substitution Using Aggregate Time Series Data," *Journal of Business and Economic Statistics*, Vol. 8, pp. 53-69.
- Eisner, Robert, 1988, "Extended Accounts for National Income Product," *Journal of Economic Literature*, Vol. 26, pp. 1611-84.
- Genay, Hesna, and Prakash Loungani, 1997, "Labor Market Fluctuations in Japan and the U.S.: How Similar Are They?" *Federal Reserve Bank of Chicago Economic Perspectives*, Vol. 21, pp. 15-28.
- Gomme, Paul, Peter Rupert, and Finn Kydland, 2001, "Time-to-Build and Household Production," *Journal of Political Economy*, Vol. 109, pp. 1115-31.
- Greenwood, Jeremy, and Zvi Hercowitz, 1991, "The Allocation of Capital and Time Over the Business Cycle," *Journal of Political Economy*, Vol. 99, pp. 1188-1214.
- Greenwood, Jeremy, Richard Rogerson, and Randall Wright, 1995 "Household Production in Real Business Cycle Theory," in *Frontiers of Business Cycle Research*, ed. by Thomas Cooley (Princeton, New Jersey: Princeton University Press), pp. 157-1745.
- Gronau, Reuben, 1986, "Home Production—A Survey," in *Handbook of Labor Economics*, ed. by Orley Ashenfelter and Richard Layard (Amsterdam: North Holland), pp. 273-304.
- Gronau, Reuben, and Daniel S. Hamermesh, 2006, "Time vs. Goods: The Value of Measuring Household Production Technologies," forthcoming in *Review of Income and Wealth*.
- Ingram, Beth, Narayana Kocherlakota, and N.E. Savin, 1994a, "Explaining Business Cycles: A Multiple Shock Approach," *Journal of Monetary Economics*, Vol. 34, pp. 415-28.
- , 1994b, "Rational Expectations Shock Estimation" (unpublished; Iowa City, Iowa: University of Iowa).
- , 1997, "Using Theory for Measurement: an Analysis of the Cyclical Behavior of Home Production," *Journal of Monetary Economics*, Vol. 40, pp. 435-56.
- Juster, F. Thomas, and Frank P. Stafford, 1991, "The Allocation of Time: Empirical Findings, Behavioral Models, and Problems of Measurement," *Journal of Economic Literature*, Vol. 29, pp. 471-522.

- Kim, Sunghyun H., and M. Ayhan Kose, 2003, "Dynamics of Open Economy Business Cycle Models: Understanding the Role of the Discount Factor," *Macroeconomic Dynamics*, Vol. 7, pp. 263-90.
- Kose, M. Ayhan, 2002, Explaining Business Cycles in Small Open Economies," *Journal of International Economics*, Vol. 56, pp. 299-327.
- Kose, M. Ayhan, Chris Otrok, and Charles Whiteman, 2003, "International Business Cycles: World Region, and Country Specific Factors," *American Economic Review*, Vol. 93, pp. 1216-39.
- Kose, M. Ayhan, and Kei-Mu Yi, 2001, "International Trade and Business Cycles," *American Economic Review*, Vol. 91, pp. 371-75.
- McGrattan, Ellen, Richard Rogerson, and Randall Wright, 1997, "An Equilibrium Model of the Business Cycle with Household Production and Fiscal Policy," *International Economic Review*, Vol. 38, pp. 267-90.
- Parente, Stephen L., Richard Rogerson, and Randall Wright, 2000, "Homework in Development Economics: Household Production and the Wealth of Nations," *Journal of Political Economy*, Vol. 108, pp. 680-87.
- Rogerson, Richard, Peter Rupert, and Randall Wright, 1995, "Estimating Substitution Elasticities in Models with Home Production," *Economic Theory*, Vol. 6, pp. 179-93.
- Siebert, Horst, 1997, "Structural Change and Labor Market Flexibility: Experience in Selected OECD Countries" (Kiel: Institute fur Weltwirtschaft an der Universitat Kiel).
- Smith, Grogor W., and Stanley E. Zin, 1997, "Real Business Cycle Realizations," *Carnegie-Rochester Series on Public Policy*, Vol. 47, pp. 243-80.
- Wrase, Jeff, 2001, "The Interplay Between Home Production and Business Activity," *Business Review of the Federal Reserve Bank of Philadelphia Q2*, pp. 23-29.
- Zimmermann, Christian, 1995, "International Trade over the Business Cycle: Stylized Facts and Remaining Puzzles," Working Paper No. 37, CREFÉ.